# CS6848 - Principles of Programming Languages

Principles of Programming Languages

#### V. Krishna Nandivada

IIT Madras



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### Outline



### Last class

#### **Interpreters**

- A Environment
- **B** Cells
- C Closures
- D Recursive environments



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## Introduction

- An interpreter executes a program as per the semantics.
- An interpreter can be viewed as an executable description of the semantics of a programming language.
- Program semantics is the field concerned with the rigorous mathematical study of the meaning of programming languages and models of computation.
- Formal ways of describing the programming semantics.
  - Operational semantics execution of programs in the language is described directly (in the context of an abstract machine).
    - Big-step semantics (with environments) -is close in spirit to the interpreters we have seen earlier.
    - Small-step semantics (with syntactic substitution) formalizes the inlining of a procedure call as an approach to computation.
  - Denotational Semantics each phrase in the language is *translated* to a *denotation* a phrase in some other language.
  - Axiomatic semantics gives meaning to phrases by describing the logical axioms that apply to them.

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### Lambda Calculus

• The traditional syntax for procedures in the lambda-calculus uses the Greek letter  $\lambda$  (lambda), and the grammar for the lambda-calculus can be written as:

 $e ::= x \mid \lambda x.e \mid e_1e_2$ 

 $x \in Identifier (infinite set of variables)$ 

- Brackets are only used for grouping of expressions. Convention for saving brackets:
  - that the body of a  $\lambda$ -abstraction extends "as far as possible."
  - For example,  $\lambda x.xy$  is short for  $\lambda x.(xy)$  and not  $(\lambda x.x)y$ .
  - Moreover,  $e_1e_2e_3$  is short for  $(e_1e_2)e_3$  and not  $e_1(e_2e_3)$ .



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### Outline

### Extension of the Lambda-calculus

We will give the semantics for the following extension of the lambda-calculus:

 $e ::= x \mid \lambda x.e \mid e_1e_2 \mid c \mid succ e$ 

 $x \in Identifier$  (infinite set of variables)

 $c \in Integer$ 



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## Big step semantics

Here is a big-step semantics with environments for the lambda-calculus.

$$w,v \in Value$$

$$v ::= c \mid \langle \lambda x.e, \rho \rangle$$

$$\rho \in Environment$$

$$\rho ::= x_1 \mapsto v_1, \dots, x_n \mapsto v_n$$

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The semantics is given by five rules:

$$\rho \vdash x \triangleright v \quad (\rho(x) = v) \tag{1}$$

$$\rho \vdash \lambda x.e \triangleright \langle \lambda x.e, \rho \rangle \tag{2}$$

$$\frac{\rho \vdash e_1 \triangleright \langle \lambda x. e, \rho' \rangle \quad \rho \vdash e_2 \triangleright v \quad \rho', x \mapsto v \vdash e \triangleright w}{\rho \vdash e_1 e_2 \triangleright w}$$
(3)

$$\rho \vdash c \triangleright c$$
(4)

$$\frac{\rho \vdash e \triangleright c_1}{\rho \vdash \operatorname{succ} e \triangleright c_2} \quad (\lceil c_2 \rceil = \lceil c_1 \rceil + 1) \tag{5}$$



### Outline



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## Small step semantics (contd.)

We can also calculate like this:

```
(foo
(+41)7)
=> (foo 5 7)
    ((lambda (x y) (+ (* x 3) y))
       5 7)
=> (+ (* 5 3) 7)
=> 22
```



## Small step semantics

- In small step semantics, one step of computation = either one primitive operation, or inline one procedure call.
- We can do steps of computation in different orders:

```
> (define foo
      (lambda (x y) (+ (* x 3) y)))
> (foo (+ 4 1) 7)
22
```

#### Let us calculate:

```
(foo (+ 4 1) 7)
   ((lambda (x y) (+ (* x 3) y))
      (+41)7)
   (+ (* (+ 4 1) 3) 7)
=> 22
```



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## Free variables

A variable *x* occurs *free* in an expression *E* iff *x* is not bound in *E*.Examples:

no variables occur free in the expression

```
(lambda (y) ((lambda (x) x) y))
```

• the variable y occurs free in the expression

```
((lambda (x) x) y)
```

An expression is *closed* if it does not contain free variables. A program is a closed expression.



## Methods of procedure application

### Call by value

```
((lambda (x) x)
((lambda (y) (+ y 9)) 5))
=> ((lambda (x) x) (+ 5 9))
=> ((lambda (x) x) 14)
=> 14
```

#### Always evaluate the arguments first

• Example: Scheme, ML, C, C++, Java



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### Difference

- Q: If we run the same program using these two semantics, can we get different results?
- A:
  - If the run with call-by-value reduction terminates, then the run with call- by-name reduction terminates. (But the converse is in general false).
  - If both runs terminate, then they give the same result.

#### Church Rosser theorem



## Methods of procedure application

#### Call by name (or lazy-evaluation)

```
((lambda (x) x)
         ((lambda (y) (+ y 9) 5))
=> ((lambda (y) (+ y 9)) 5)
=> (+59)
=> 14
```

#### Avoid the work if you can

Example: Miranda and Haskell

Lazy or eager: Is one more efficient? Are both the same?



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## Call by value - too eager?

Sometimes call-by-value reduction fails to terminate, even though call-by- name reduction terminates.

```
(define delta (lambda (x) (x x)))
    (delta delta)
=> (delta delta)
    (delta delta)
```

#### Consider the program:

```
(const (delta delta))
(define const (lambda (v) 7))
```

- call by value reduction fails to terminate; cannot finish evaluating the operand.
- call by name reduction terminates.

### Beta reduction

- call by value is more efficient but may not terminate
- call by name may evaluate the same expression multiple times.
- Lazy languages uses call-by-need.
- Languages like Scala allow both call by value and name!



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A procedure call which is ready to be "inlined" is called a

• The process of inlining a beta-redex for some reducible

the choosing of arbitrary beta-redex.

expression is called beta-reduction.

beta-redex. Example ( (lambda (var) body ) rand )

• In lambda-calculus call-by-value and call-by-name reduction allow

( (lambda (var) body ) rand ) body[var:=rand]

### Name clashes

• Care must be taken to avoid name clashes. Example:

```
((lambda (x))
   (lambda (y) (y x))
 (y 5)
```

should not be transformed into

```
(lambda (y) (y (y 5)))
```

- The reference to y in (y 5) should remain free!
- $\bullet$  The solution is to change the name of the inner variable name y to some name, say z, that does not occur free in the argument y = 5.

```
((lambda (x)
   (lambda (z) (z x))
 (y 5)
```



- (lambda (z) (z (y x))); the y present.

## Substitution

- The notation e[x := M] denotes e with M substituted for every free occurrence of x in such that a way that name clashes are avoided.
- We will define e[x := M] inductively on e.

$$\begin{array}{lll} x[x:=M] & \equiv & M \\ y[x:=M] & \equiv & y \, (x \neq y) \\ (\lambda x.e_1)[x:=M] & \equiv & (\lambda x.e_1) \\ (\lambda y.e_1)[x:=M] & \equiv & \lambda z.((e_1[y:=z])[x:=M]) \\ & & (\text{where } x \neq y \text{ and } z \text{ does not occur free in } e_1 \text{ or } M). \\ (e_1e_2)[x:=M] & \equiv & (e_1[x:=M])(e_2[x:=M]) \\ c[x:=M] & \equiv & c \\ (succ\ e_1)[x:=M] & \equiv & succ\ (e_1[x:=M]) \end{array}$$

alpha-conversion.

• The renaming of a bound variable by a fresh variable is called

# Small step semantics

Here is a small-step semantics with syntactic substitution for the  $\lambda$ -calculus.

$$v \in Value$$
  
 $v ::= c \mid \lambda x.e$ 

The semantics is given by the reflexive, transitive closure of the relation  $\rightarrow_{\mathcal{V}}$ :

 $\rightarrow_V \subseteq Expression \times Expression$ 

$$(\lambda x.e)v \to_V e[x := v] \tag{6}$$

$$\frac{e_1 \to_V e_1'}{e_1 e_2 \to_V e_1' e_2} \tag{7}$$

$$\frac{e_2 \to_V e_2'}{v \ e_2 \to_V v \ e_2'} \tag{8}$$

$$\operatorname{succ} c_1 \to_V c_2 \quad (\lceil c_2 \rceil = \lceil c_1 \rceil + 1) \tag{9}$$

$$\frac{e_1 \to_V e_2}{\operatorname{succ} e_1 \to_V \operatorname{succ} e_2} \tag{10}$$



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# Things to Do

- No class on Friday.
- Meet the TA and get any doubts regarding the Assignment 1 cleared.
- Prepare your snipers.



## Health card

- A Big step semantic
- **B** Calling convention
- C Small step semantics
- 4: Can teach myself, 3: Can teach with help, 2: Need a bit of help, 1: No clue.



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It's a shame the world is so full of conflict.

On the other hand, I'm a lawyer.

Faculty of IITM!

