CS3300 - Language Translators Liveness analysis and Register allocation

V. Krishna Nandivada

IIT Madras

Copyright © 2012 by Antony L. Hosking. Permission to make digital or hard copies of part or all of this work for personal or classroom use is granted without fee provided that copies are not made or distributed for profit or commercial advantage and that copies bear this notice and full citation on the first page. To copy otherwise, to republish, to post on servers, or to redistribute to lists, requires prior specific permission and/or fee. Request permission to publish from hosking@cs.purdue.edu.

CS3300 - Aug 2012



Register allocation



Register allocation:

- have value in a register when used
- limited resources
- can effect the instruction choices
- can move loads and stores
- optimal allocation is difficult
 - \Rightarrow NP-complete for $k \ge 1$ registers

Liveness analysis

V.Krishna Nandivada (IIT Madras)

Problem:

- IR contains an unbounded number of temporaries
- machine has bounded number of registers

Approach:

- temporaries with disjoint live ranges can map to same register
- if not enough registers then <u>spill</u> some temporaries (i.e., keep them in memory)
- The compiler must perform liveness analysis for each temporary:

It is <u>live</u> if it holds a value that may be needed in future



 $a \leftarrow 0$ $L_1: \quad b \leftarrow a+1$ $c \leftarrow c+b$ $a \leftarrow b \times 2$ if a < N goto L_1 return c

V.Krishna Nandivada (IIT Madras) CS3300 - Aug 2012 5/25

Definitions

- v is live on edge e if there is a directed path from e to a use of v that does not pass through any def(v)
- *v* is live-in at node *n* if live on any of *n*'s in-edges
- v is live-out at n if live on any of n's out-edges
- $v \in USe[n] \Rightarrow v$ live-in at n
- *v* live-in at $n \Rightarrow v$ live-out at all $m \in pred[n]$
- *v* live-out at $n, v \notin def[n] \Rightarrow v$ live-in at n

Liveness analysis

Gathering liveness information is a form of $\underline{\text{data flow analysis}}$ operating over the CFG:

- We will treat each statement as a different basic block.
- liveness of variables "flows" around the edges of the graph
- assignments define a variable, v:
 - def(v) = set of graph nodes that define v
 - def[n] = set of variables defined by n
- occurrences of v in expressions <u>use</u> it:
 - Use(v) = set of nodes that use v
 - Use[n] = set of variables used in n



CS3300 - Aug 2012

6/25

Liveness analysis

Define:

```
in[n] = variables live-in at n
out[n] = variables live-out at n
```

Then:

$$out[n] = \bigcup_{s \in succ(n)} in[s]$$

 $succ[n] = \phi \Rightarrow out[n] = \phi$

Note:

 $in[n] \supseteq use[n]$ $in[n] \supseteq out[n] - def[n]$

use[n] and def[n] are constant (independent of control flow) Now, $v \in in[n]$ iff. $v \in use[n]$ or $v \in out[n] - def[n]$ Thus, $in[n] = use[n] \cup (out[n] - def[n])$ VKrishna Nandivada (IIT Madras)



N: Set of nodes of CFG;foreach $\underline{n \in N}$ do $\begin{vmatrix} in[n] \leftarrow \phi; \\ out[n] \leftarrow \phi; \\ end \\ \text{repeat} \\ \end{vmatrix}$ foreach $\underline{n \in \text{Nodes }}$ do $\begin{vmatrix} in'[n] \leftarrow in[n]; \\ out'[n] \leftarrow out[n]; \\ in[n] \leftarrow use[n] \cup (out[n] - def[n]); \\ out[n] \leftarrow \bigcup_{s \in succ[n]} in[s]; \\ end \\ \text{until } \forall n, in'[n] = in[n] \lor out'[n] = out[n]; \\ \end{vmatrix}$

Notes

- should order computation of inner loop to follow the "flow"
- liveness flows backward along control-flow arcs, from out to in
- nodes can just as easily be basic blocks to reduce CFG size
- could do one variable at a time, from <u>uses</u> back to <u>defs</u>, noting liveness along the way

CS3300 - Aug 2012

0/2

Iterative solution for liveness

Complexity: for input program of size N

• $\leq N$ nodes in CFG

V.Krishna Nandivada (IIT Madras)

- $\Rightarrow \leq N$ variables
- \Rightarrow N elements per *in/out*
- \Rightarrow O(N) time per set-union
- for loop performs constant number of set operations per node $\Rightarrow O(N^2)$ time for for loop

CS3300 - Aug 2012

- each iteration of **repeat** loop can only add to each set sets can contain at most every variable
 - \Rightarrow sizes of all in and out sets sum to $2N^2$,
 - bounding the number of iterations of the repeat loop
- \Rightarrow worst-case complexity of O(N^4)
- ordering can cut **repeat** loop down to 2-3 iterations $\Rightarrow O(N)$ or $O(N^2)$ in practice



Least fixed points

V.Krishna Nandivada (IIT Madras)

There is often more than one solution for a given dataflow problem (see example).

Any solution to dataflow equations is a conservative approximation:

• v has some later use downstream from n

 $\Rightarrow v \in out(n)$

but not the converse

Conservatively assuming a variable is live does not break the program; just means more registers may be needed.

Assuming a variable is dead when really live will break things.

Many possible solutions but we want the "smallest": the least fixpoint. The iterative algorithm computes this least fixpoint.



• Step 1:

- Select target machine instructions assuming infinite registers (temps).
- If a instruction requires a special register replace that temp with that register.
- Step 2:
 - Construct an interference graph.
 - Solve the register allocation problem by coloring the graph.
 - A graph is said to be <u>colored</u> if each each pair of neighboring nodes have different colors.

V.Krishna Nandivada (IIT Madras)	CS3300 - Aug 2012	13 / 25

Example 1, available colors = 2

Graph coloring - a simplistic approach

Input: *G* - the interference graph, *K* - number of colors **repeat**

repeat

- Remove a node n and all its edges from G, such that degree of n is less than K;
- Push *n* onto a stack;

until <u>G</u> has no node with degree less than K;

// G is either empty or all of its nodes have degree \geq K

if G is not empty then

- Take one node *m* out of *G*, and mark it for spilling;
- Remove all the edges of m from G;

end

until G is empty;

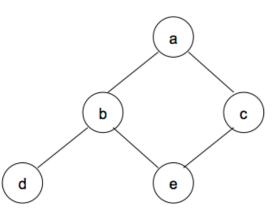
Take one node at a time from the stack and assign a non conflicting color.



CS3300 - Aug 2012

14/25

Example 2



We have to spill.

Graph coloring - Kempe's heuristic

• Algorithm dating back to 1879.

Input: *G* - the interference graph, *K* - number of colors **repeat**

repeat

Remove a node n and all its edges from G, such that degree of n is less than K;

Push *n* onto a stack;

until \underline{G} has no node with degree less than K;

// G is either empty or all of its nodes have degree \geq K

if G is not empty then

Take one node m out of G.;

push *m* onto the stack;

end

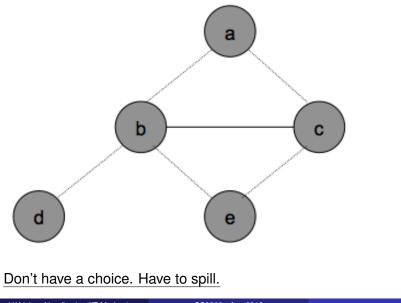
until G is empty;

Take one node at a time from the stack and assign a non conflicting color (1) possible, else spill).

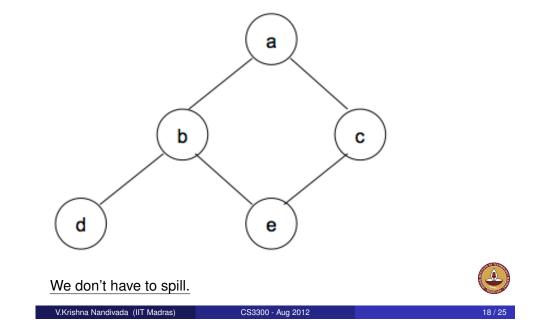
```
V.Krishna Nandivada (IIT Madras)
```

CS3300 - Aug 2012

Example 3



Example 2 (revisited)



Register allocation - Linear scan

Register allocation is **expensive**.

- Many algorithms use heuristics for graph coloring.
- Allocation may take time quadratic in the number of live intervals.

Not suitable

- Online compilers need to generate code quickly. e.g. JIT compilers.
- Sacrifice efficient register allocation for compilation speed.

Linear scan register allocation - Massimiliano Poletto and Vivek Sarkar, ACM TOPLAS 1999



Linear Scan algorithm

LINEARSCANREGISTERALLOCATION $active \leftarrow \{\}$	
foreach live interval i , in order of increasing start point	
EXPIREOLDINTERVALS (i)	
if $length(active) = R$ then	
${ m SpillAtInterval}(i)$	
else	
$register[i] \leftarrow$ a register removed from pool of free registers	
add i to <i>active</i> , sorted by increasing end point	
ExpireOldIntervals (i)	
foreach interval j in <i>active</i> , in order of increasing end point	
$\mathbf{if} endpoint[j] \geq startpoint[i] \mathbf{then}$	
return	
remove j from <i>active</i>	
add $register[j]$ to pool of free registers	
SPILLATINTERVAL(i)	
$spill \leftarrow last interval in active$	
if $endpoint[spil] > endpoint[i]$ then	
$register[i] \leftarrow register[spil]$	
$location[spill] \leftarrow new stack location$	
remove spill from active	A DECEMBER OF A
add i to <i>active</i> , sorted by increasing end point	
else	
$location[i] \leftarrow \text{new stack location}$	Com Die
V.Krishna Nandivada (IIT Madras) CS3300 - Aug 2012	21 / 25

Linear Scan algorithm - analysis

- Each live range gets either a register or a spill location.
- Note: The number of overlapping intervals changes only at the start and end points of an interval.
- Live intervals are stored in a list that is sorted in order of increasing start point.
- The <u>active</u> list is kept sorted in order of increasing end point. Adv: need to scan only those intervals (+1 at most) that have to be removed.
- Complexity: O(V) if number of registers is assumed ot be a constant. Else? O(V × logR)

Example



Spilling

- We need to generate extra instructions to load variables from the stack and store them back.
- The load and store may require registers again:
 - Naive approach: Keep a separate register (wasteful).
 - Rewrite the code by introducing a temporary; rerun the liveness + ra.

(Note: the new temp has much smaller live range).



Consider: add t1 t2

- Suppose t2 has to be spilled, say to [sp-4].
- Invent a new temp t35, and rewrite:
 - mov t35 [sp-4] add t1 t35
- t35 has a very short live range and less likely to interfere.
- Now rerun the algo.

Criteria for spilling

During register allocation, we identify that one of the live ranges from a given set, has to be spilled. Criteria?

CS3300 - Aug 2012

- Random! Adv? Disadv?
- One with maximum degree
- One that has the longest life
- One with the shortest life (take advantage of the cache).
- One with least cost.

V.Krishna Nandivada (IIT Madras)

- Cost = Dynamic (load cost + store cost)
- How to handle loops, conditionals?
- Cost of load, store



Caller and Callee save registers

- The set of registers are divided into caller save and callee save registers.
- Caller has three choices: Save callee save registers, caller save registers or all.
- Callee has three choices: Save caller save registers, callee save registers or all.

Adv and Disadv?

