#### CS3300 - Language Translators Liveness analysis and Register allocation

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# Register allocation



Register allocation:

- have value in a register when used
- limited resources
- can effect the instruction choices
- can move loads and stores
- optimal allocation is difficult
  - $\Rightarrow$  NP-complete for  $k \ge 1$  registers

#### Liveness analysis

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Problem:

- IR contains an unbounded number of temporaries
- machine has bounded number of registers

Approach:

- temporaries with disjoint live ranges can map to same register
- if not enough registers then <u>spill</u> some temporaries (i.e., keep them in memory)
- The compiler must perform liveness analysis for each temporary:

It is <u>live</u> if it holds a value that may be needed in future



 $a \leftarrow 0$   $L_1: \quad b \leftarrow a+1$   $c \leftarrow c+b$   $a \leftarrow b \times 2$ if a < N goto  $L_1$ return c

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# Definitions

- v is live on edge e if there is a directed path from e to a use of v that does not pass through any def(v)
- *v* is live-in at node *n* if live on any of *n*'s in-edges
- v is live-out at n if live on any of n's out-edges
- $v \in USe[n] \Rightarrow v$  live-in at n
- *v* live-in at  $n \Rightarrow v$  live-out at all  $m \in pred[n]$
- *v* live-out at  $n, v \notin def[n] \Rightarrow v$  live-in at n

# Liveness analysis

Gathering liveness information is a form of  $\underline{\text{data flow analysis}}$  operating over the CFG:

- We will treat each statement as a different basic block.
- liveness of variables "flows" around the edges of the graph
- assignments define a variable, v:
  - def(v) = set of graph nodes that define v
  - def[n] = set of variables defined by n
- occurrences of v in expressions <u>use</u> it:
  - Use(v) = set of nodes that use v
  - Use[n] = set of variables used in n



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# Liveness analysis

Define:

```
in[n] = variables live-in at n
out[n] = variables live-out at n
```

Then:

$$out[n] = \bigcup_{s \in succ(n)} in[s]$$
  
 $succ[n] = \phi \Rightarrow out[n] = \phi$ 

Note:

 $in[n] \supseteq use[n]$  $in[n] \supseteq out[n] - def[n]$ 

use[n] and def[n] are constant (independent of control flow) Now,  $v \in in[n]$  iff.  $v \in use[n]$  or  $v \in out[n] - def[n]$ Thus,  $in[n] = use[n] \cup (out[n] - def[n])$ VKrishna Nandivada (IIT Madras)



# N: Set of nodes of CFG;foreach $\underline{n \in N}$ do $\begin{vmatrix} in[n] \leftarrow \phi; \\ out[n] \leftarrow \phi; \\ end \\ \text{repeat} \\ \end{vmatrix}$ foreach $\underline{n \in \text{Nodes }}$ do $\begin{vmatrix} in'[n] \leftarrow in[n]; \\ out'[n] \leftarrow out[n]; \\ in[n] \leftarrow use[n] \cup (out[n] - def[n]); \\ out[n] \leftarrow \bigcup_{s \in succ[n]} in[s]; \\ end \\ \text{until } \forall n, in'[n] = in[n] \lor out'[n] = out[n]; \\ \end{vmatrix}$

#### Notes

- should order computation of inner loop to follow the "flow"
- liveness flows backward along control-flow arcs, from out to in
- nodes can just as easily be basic blocks to reduce CFG size
- could do one variable at a time, from <u>uses</u> back to <u>defs</u>, noting liveness along the way

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# Iterative solution for liveness

Complexity: for input program of size N

•  $\leq N$  nodes in CFG

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- $\Rightarrow \leq N$  variables
- $\Rightarrow$  N elements per *in/out*
- $\Rightarrow$  O(N) time per set-union
- for loop performs constant number of set operations per node  $\Rightarrow O(N^2)$  time for for loop

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- each iteration of **repeat** loop can only add to each set sets can contain at most every variable
  - $\Rightarrow$  sizes of all in and out sets sum to  $2N^2$ ,
  - bounding the number of iterations of the repeat loop
- $\Rightarrow$  worst-case complexity of O( $N^4$ )
- ordering can cut **repeat** loop down to 2-3 iterations  $\Rightarrow O(N)$  or  $O(N^2)$  in practice



#### Least fixed points

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There is often more than one solution for a given dataflow problem (see example).

Any solution to dataflow equations is a conservative approximation:

• v has some later use downstream from n

 $\Rightarrow v \in out(n)$ 

but not the converse

Conservatively assuming a variable is live does not break the program; just means more registers may be needed.

Assuming a variable is dead when really live will break things.

Many possible solutions but we want the "smallest": the least fixpoint. The iterative algorithm computes this least fixpoint.



#### • Step 1:

- Select target machine instructions assuming infinite registers (temps).
- If a instruction requires a special register replace that temp with that register.
- Step 2:
  - Construct an interference graph.
  - Solve the register allocation problem by coloring the graph.
  - A graph is said to be <u>colored</u> if each each pair of neighboring nodes have different colors.

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# Example 1, available colors = 2

# Graph coloring - a simplistic approach

**Input**: *G* - the interference graph, *K* - number of colors **repeat** 

#### repeat

- Remove a node n and all its edges from G, such that degree of n is less than K;
- Push *n* onto a stack;

#### **until** <u>G</u> has no node with degree less than K;

// G is either empty or all of its nodes have degree  $\geq$  K

#### if G is not empty then

- Take one node *m* out of *G*, and mark it for spilling;
- Remove all the edges of m from G;

#### end

#### until G is empty;

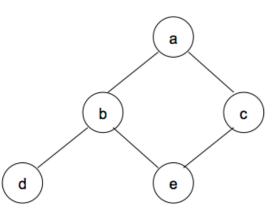
Take one node at a time from the stack and assign a non conflicting color.



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# Example 2



#### We have to spill.

# Graph coloring - Kempe's heuristic

• Algorithm dating back to 1879.

**Input**: *G* - the interference graph, *K* - number of colors **repeat** 

#### repeat

Remove a node n and all its edges from G, such that degree of n is less than K;

Push *n* onto a stack;

#### **until** $\underline{G}$ has no node with degree less than K;

// G is either empty or all of its nodes have degree  $\geq$  K

#### if G is not empty then

Take one node m out of G.;

push *m* onto the stack;

#### end

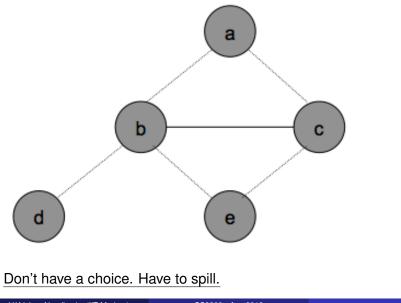
#### until G is empty;

Take one node at a time from the stack and assign a non conflicting color (1) possible, else spill).

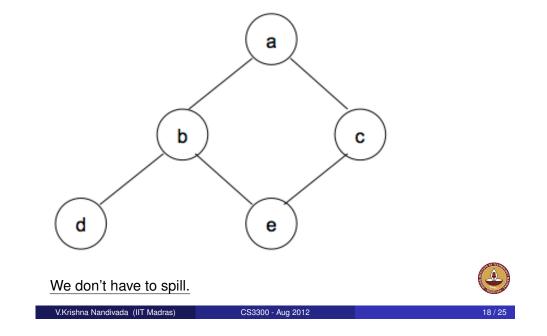
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```

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# Example 3



# Example 2 (revisited)



# Register allocation - Linear scan

Register allocation is **expensive**.

- Many algorithms use heuristics for graph coloring.
- Allocation may take time quadratic in the number of live intervals.

#### Not suitable

- Online compilers need to generate code quickly. e.g. JIT compilers.
- Sacrifice efficient register allocation for compilation speed.

Linear scan register allocation - Massimiliano Poletto and Vivek Sarkar, ACM TOPLAS 1999



# Linear Scan algorithm

LINEARSCANREGISTERALLOCATION $active \leftarrow \{\}$	
<b>foreach</b> live interval $i$ , in order of increasing start point	
EXPIREOLDINTERVALS $(i)$	
if $length(active) = R$ then	
${ m SpillAtInterval}(i)$	
else	
$register[i] \leftarrow$ a register removed from pool of free registers	
add $i$ to <i>active</i> , sorted by increasing end point	
ExpireOldIntervals $(i)$	
foreach interval $j$ in <i>active</i> , in order of increasing end point	
$\mathbf{if} endpoint[j] \geq startpoint[i] \mathbf{then}$	
return	
remove $j$ from <i>active</i>	
add $register[j]$ to pool of free registers	
SPILLATINTERVAL(i)	
$spill \leftarrow last interval in active$	
if $endpoint[spil] > endpoint[i]$ then	
$register[i] \leftarrow register[spil]$	
$location[spill] \leftarrow new stack location$	
remove spill from active	A DECEMBER OF A
add $i$ to <i>active</i> , sorted by increasing end point	
else	
$location[i] \leftarrow \text{new stack location}$	Com Die
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# Linear Scan algorithm - analysis

- Each live range gets either a register or a spill location.
- Note: The number of overlapping intervals changes only at the start and end points of an interval.
- Live intervals are stored in a list that is sorted in order of increasing start point.
- The <u>active</u> list is kept sorted in order of increasing end point. Adv: need to scan only those intervals (+1 at most) that have to be removed.
- Complexity: O(V) if number of registers is assumed ot be a constant. Else? O(V × logR)

# Example



#### Spilling

- We need to generate extra instructions to load variables from the stack and store them back.
- The load and store may require registers again:
  - Naive approach: Keep a separate register (wasteful).
  - Rewrite the code by introducing a temporary; rerun the liveness + ra.

(Note: the new temp has much smaller live range).



#### **Consider:** add t1 t2

- Suppose t2 has to be spilled, say to [sp-4].
- Invent a new temp t35, and rewrite:
  - mov t35 [sp-4] add t1 t35
- t35 has a very short live range and less likely to interfere.
- Now rerun the algo.

# Criteria for spilling

During register allocation, we identify that one of the live ranges from a given set, has to be spilled. Criteria?

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- Random! Adv? Disadv?
- One with maximum degree
- One that has the longest life
- One with the shortest life (take advantage of the cache).
- One with least cost.

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- Cost = Dynamic (load cost + store cost)
- How to handle loops, conditionals?
- Cost of load, store



# Caller and Callee save registers

- The set of registers are divided into caller save and callee save registers.
- Caller has three choices: Save callee save registers, caller save registers or all.
- Callee has three choices: Save caller save registers, callee save registers or all.

Adv and Disadv?

