

How the high level specifications are mapped.

Goal: Identify patterns in each stage.

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A pattern language

Supporting Structures

Implementation Mechanisms



- Task decomposition: A program to a sequence of "tasks".
 - Some of the tasks can run in parallel.
 - Independent the tasks the better.
- Data decomposition: Focus on the data used by the program. Decompose the program into tasks based on distinct chunks of data.
 - Efficiency depends on the independence of the chunks.
- Task decomposition may lead to data decomposition and vice versa.

Q: Are they really independent?



Task decomposition: Matrix multiplication example

$$C = A imes B$$

$$C_{i,j} = \sum_{k=0}^{N-1} A_{i,k} \times B_{k,j}$$

- "Resource" intensive parts?
- Tasks in the problem?
- Are tasks independent? Enough tasks for all the cores? Enough work for each task? Size of tasks and number of cores?
- Each element $C_{i,j}$ is computed in a different task row major.
- Each element $C_{i,j}$ is computed in a different task column major.
- Each element C_{i,j} is computed in a different task diagonals.
- How to reason about Performance? Cache effect?

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Task decomposition: An approach

- Identify "resource" intensive parts of the problem.
- Identify different tasks that make up the problem. Challenge: write the algorithms and run the tasks concurrently.
- Sometimes the problem will naturally break into a collection of (nearly) independent tasks. Sometimes, not!
- Q: Are there enough tasks to keep the map all the H/W cores?
- Q: Does each task have enough work to keep the individual cores busy?
- Q: Are the number of tasks dependent or independent of the number of H/W core?
- Q: Are these tasks relatively independent?
- Instances of tasks: Independent modules, loop iterations.
- Relation between tasks and ease of programming, debugging and maintenance.

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Finding concurrency in a given problem



Data decomposition: Design

- Besides identifying the "resource" intensive parts, identify the key data structures required to solve the problem, and how is the data used during the solution.
- Q: Is the decomposition suitable to a specific system or many systems?
- Q: Does it scale with the size of parallel computer?
- Are similar operations applied to different parts of data, independently?
- Are there different chunks of data that can be distributed?
- Relation between decomposition and ease of programming, debugging and maintenance.
- Examples:
 - Array based computations: concurrency defined in terms of updates of different segments of the array/matrix.
 - Recursive data structures: concurrency by decomposing the parallel updates of a large tree/graph/linked list.

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Matrix multiplication: Data decomposition.

$$C = \begin{pmatrix} A_{1,1} & A_{1,2} \\ A_{2,1} & A_{2,2} \end{pmatrix} \times \begin{pmatrix} B_{1,1} & B_{1,2} \\ B_{2,1} & B_{2,2} \end{pmatrix}$$
$$= \begin{pmatrix} A_{1,1} \times B_{1,1} + A_{1,2} \times B_{2,1} & A_{1,1} \times B_{1,2} + A_{1,2} \times B_{2,2} \\ A_{2,1} \times B_{1,1} + A_{2,2} \times B_{2,1} & A_{2,1} \times B_{1,2} + A_{2,2} \times B_{2,2} \end{pmatrix}$$

Advantages

- Can fit in the blocks into cache.
- Can scale as per the hardware.
- Overlap of communication and computation.

Data decomposition: Matrix multiplication example



$$C_{i,j} = \sum_{k=0}^{N-1} A_{i,k} imes B_{k,j}$$

- "Resource" intensive parts?
- Data chunks in the problem?
- Does it scale with the size of parallel computers?
- Operations (Reads/Writes) applied on independent parts of data?
- Data chunks big enough to deem the thread activity beneficial?
- How to decompose?
- Each row/column of *C_{i,j}* is computed in a different task.
- Each column of $C_{i,j}$ is computed in a different task.
- Performance? Cache effect?
- Note: Data decomposition also leads to task decomposition as
 well.

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Finding concurrency in a given problem



Dependence analysis for managing parallelism: Grouping

- Background: Tasks and Data decomposition has been done.
- All the identified tasks may not run in parallel.
- **Q**: How should related tasks be grouped to help manage the dependencies?
- Dependent, related tasks should be (uniquely?) grouped together.
 - Temporal dependency: If task A depends on the result of task *B*, then *A* must wait for the results from *B*. Q: Does *A* have to wait for *B* to terminate?
 - Concurrent dependency: Tasks are expected to run in parallel, and one depends on the updates of the other.
 - Independent tasks: Can run in parallel or in sequence. Is it always better to run them in parallel?
- Advantage of grouping.
 - Grouping enforces partial orders between tasks.
 - Application developer thinks of groups, instead of individual task
- Example: Computing of individual rows.

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Dependence analysis for managing parallelism: data sharing

Background: Tasks and Data decomposition has been done. Dependent tasks have been grouped together. The ordering between the groups and tasks have been identified.

- Groups and tasks have some level of dependency among each other.
- Q: How is data shared among the tasks?
- Identify the data updated/needed by individual tasks task local data.
- Some data may be updated by multiple tasks global data.
- Some data may be updated by one data used by multiple tasks remote data

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Dependence analysis for managing parallelism: Ordering

- **Background**: Tasks and Data decomposition has been done. Dependent tasks have been grouped together.
- Ordering of the tasks and groups not trivial.
- **Q**: How should the groups be ordered to satisfy the constraints among the groups and in turn tasks?
- Dependent groups+tasks should be ordered to preserve the original semantics.
 - Should not be overly restrictive.
 - Ordering is imposed by: Data + Control dependencies.
 - Ordering can also be imposed by external factors: network, i/o and so on.
 - Ordering of independent tasks?
- Importance of grouping.
 - Ensures the program semantics.
 - A key step in program design.

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Issues in data sharing

- Identify the data being shared directly follows from the decomposition.
- If sharing is done incorrectly a task may get invalid data due to race condition.
- A naive way to guarantee correct shared data: synchronize every read with barriers.
- Synchronization of data across different tasks may require communication. Options:
 - Overlap of communication and computation.
 - Privatization.
 - keep local copies of shared data.

Finding concurrency in a given problem - deep dive

- Accumulation/Reduction: Data being used to accumulate a result; sum, minimum, maximum, variance etc.
 - Each core has a separate copy of data,
 - accumulation happens in these local copies.
 - sub-results are further used to compute the final result.
- Example: Sum elements in an array A[1024]
 - Decompose the array into 32 chunk.
 - Accumulate each chunk separately.
 - Accumulate the sub results into the global "sum".

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Managing parallelism - design evaluation

Background: Tasks and Data decomposition has been done. Dependent tasks have been grouped together. The ordering between the groups and tasks have been identified. A scheme for data sharing has also been identified.

- Of the multiple choices present at different points, we have chosen one.
- **Q**: Is the chosen path a "good" one?



Design evaluation factors

- Suitability to the target platform (at a high level)
 - Number of cores / HW threads too few/many tasks?
 - Homogeneous/Heterogeneous multi-cores? And work distribution.
 - Data distribution among the cores equal/unequal?
 - Cost of communication fine/coarse grained data sharing.
 - Amount of sharing shared memory or distributed memory.
- Metrics: simplicity (qualitative), Efficiency, Flexibility
- Flexibility
 - Flexible/Parametric over the number of cores/threads?
 - Flexible/Parametric over the number and size of data chunks?
 - Does it handle boundary cases?
- Efficiency.
 - Even load balancing?
 - Minimum overhead? task creation, synchronization, communication.







Algorithm Structure design



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Task Parallelism

Q: A problem is best decomposed into a collection of tasks that can execute concurrently. How to exploit the concurrency efficiently?

- Problem can be decomposed into a collection of concurrent tasks.
- Tasks can be completely independent or can have dependencies.
- Tasks can be known from the beginning (producer/consumer), tasks are created dynamically.
- Solution may or not require all the tasks to finish.

Challenges:

- Assign tasks to cores to result in a simple, flexible and efficient execution.
- Address the dependencies correctly.



Factors in efficient Task parallel algorithm design

Tasks:

- Enough Tasks to keep the cores busy.
- Advantage of creating the tasks should offset the overhead of creating and managing them.
- Dependencies

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- Ordering constraints.
- Dependencies from shared data: synchronization, private data.
 Schedule: creation and scheduling.
- Schedule
 - How are the tasks assigned to cores.
 - e How are the tasks scheduled.



Example: Task parallel algorithm

Machine	Job1	Job2	Job3	Job4
M1	4	4	3	5
M2	2	3	4	4



Algorithm Structure design



Solution to Branch and Bound ILP

- Maintain a list of tasks.
- Remove a solution from the list.
- Examine the solution. Either discard it or declare it a solution, or add a sub-problem to task list.
- The tasks depend depend on each other through the task-list.

Divide and conquer

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Q: Tasks are created recursively to solve a problem in a divide conquer strategy. How to exploit the concurrency?

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- Divide and Conquer: Problem is solved by splitting it into a number of smaller subproblems. Examples?
- Each subproblems can be solved "fairly" independently. Directly or further divide and conquer.
- Solutions of the smaller problems is merged to compute the final solution.
- Each divide doubles the concurrency.
- Each merge halves the concurrency.



Divide and Conquer pattern: features



- The amount of exploitable concurrency varies.
- At the beginning and end very little exploitable concurrency.
- Note: "split" and "merge" are serial parts.
- Amdahl's law speed up constrained by the serial part. Impact?
- Too many parallel threads?
- What if cores are distributed? data movement?
- Tasks are created dynamically load balancing?
- What if the sub-problems are not equal-sized?

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Algorithm Structure design





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Divide and conquer - example Mergesort

```
int[] mergesort(int[]A, int L, int H){
    if (H - L <= 1) return;
    if (H-L <= T) {quickSort(A, L, H); return;}
    int m = (L+H)/2;
    A1 = mergesort(A, L, m);
    A2 = mergesort(A, m+1, H);
    return merge(A1, A2);
    // returns a merged sorted array.
}</pre>
```

- split cost?
- merge cost?
- Value of threshold T?

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Geometric decomposition

Q: How can an algorithm be organized around a data structure that has been decomposed into concurrently updatable "chunks"?

- Similar to decomposing a geometric region into subregions.
- Linear Data structures (such as arrays) can be often decomposed into contiguous sub-structures.
- These individual tasks are processed in different concurrent tasks.
- Note: Sometimes all the required data for a task is present "locally" (embarrassingly parallel - Task parallelism pattern). And sometimes share data with "neighboring" chunks.

Challenges

- Ensure that each task has access to all data it needs.
- Mapping of chunks to cores giving good performance. Q: Why is it a challenge?
- Granularity of decomposition (coarse or fine-grain) effect on efficiency? Parametric? Tweaked at compile time or runtime?

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• Shape of the chunk: Regular/irregular?



$$C = A \times B$$

= $\begin{pmatrix} A_{1,1} & A_{1,2} \\ A_{2,1} & A_{2,2} \end{pmatrix} \times \begin{pmatrix} B_{1,1} & B_{1,2} \\ B_{2,1} & B_{2,2} \end{pmatrix}$
= $\begin{pmatrix} A_{1,1} \times B_{1,1} + A_{1,2} \times B_{2,1} & A_{1,1} \times B_{1,2} + A_{1,2} \times B_{2,2} \\ A_{2,1} \times B_{1,1} + A_{2,2} \times B_{2,1} & A_{2,1} \times B_{1,2} + A_{2,2} \times B_{2,2} \end{pmatrix}$





Recursive Data Pattern

Q: How can recursive data structures be partitioned so as that operations on them are performed in parallel?

- Linked list, tree, graphs ...
- Inherently operations on recursive data structures are serial as one has to sequentially move through the data structure.
- For example linked list traversal or traversing a binary tree.
- Sometimes it is possible to reshape operations to derive and exploit concurrency.



Recursive Data Pattern - example Find roots



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- Given a forest of rooted trees: compute the root of each node.
- Serial version: Do a depth-first or breadth first traversal from root to the leaf nodes.
- For each visited node set the root. Total running time?

Q: Is there concurrency?

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Recursive Data structures: Parallel find roots



- Transformed the original serial computation to one where we compute partial result and repeatedly combine partial results. Total Cost = ?
- Total cost = $O(N \log N)$
- However, if we exploit the parallelism running time will come down to $O(\log N)$.

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Algorithm Structure design





- Recasting the problem increases the cost. Find a way to get it back.
- Effective exploitation of the derived concurrency depends on factors such as amount of work available for each task, amount of serial code ...
- Restructuring may make the solution complex.
- Requirement of synchronization Why?
- Another example: Find partial sums in a linked list.

ſ	x0	x1	x2	x3	x4	x5	x6	x7
	•+•	• • •	• • •	•	• • •	• • •	· • · · ·	• •
1	•	· ·	•	• •	• •	•	· · /	•

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Pipieline pattern

Q: The computation may involve performing similar sets of operations on many sets of data. Is there concurrency? How to exploit it?

• Factory assembly line, Network Packet processing, Instruction processing in CPUs etc.

	time
pipeline stage 1	C_1 C_2 C_3 C_4 C_5 C_6
pipeline stage 2	$\begin{bmatrix} C_1 \end{bmatrix} \begin{bmatrix} C_2 \end{bmatrix} \begin{bmatrix} C_3 \end{bmatrix} \begin{bmatrix} C_4 \end{bmatrix} \begin{bmatrix} C_5 \end{bmatrix} \begin{bmatrix} C_6 \end{bmatrix}$
pipeline stage 3	$egin{array}{cccccccccccccccccccccccccccccccccccc$
pipeline stage 4	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$

- There are ordering constraints on each operation on any one set of data: Operation *C*₂ can be undertaken only after *C*₁.
- Key requirement: Number of operations > 1.

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Pipeline pattern features

	time
pipeline stage 1	$egin{array}{cccccccccccccccccccccccccccccccccccc$
pipeline stage 2	$egin{array}{cccccccccccccccccccccccccccccccccccc$
pipeline stage 3	$egin{array}{cccccccccccccccccccccccccccccccccccc$
pipeline stage 4	$egin{array}{c c} \hline C_1 & \hline C_2 & \hline C_3 & \hline C_4 & \hline C_5 & \hline C_6 & \hline \end{array}$

- Once the pipeline is full maximum parallelism is observed.
- Number of stages should be small compared to the number of items processed.
- Efficiency improves if time taken in each stage is roughly the same. Else?
- Amount of concurrency depends on the number of stages.
- Too many stages, disadvantage?
- Communication across stages?

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Overall big picture



Pipieline pattern. Issues

- Error handling.
 - Create a separate task for error handling which will run exception routines.

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- Processor allocation, load balancing
- Throughput and Latency.

Event based coordination

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- Identifying the events flow.
- Enforcing the events ordering.
- Avoiding deadlock.
- Efficient communication of events.

Left for self reading.



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SPMD pattern

- Each UE executes the same program, but has different data.
- They can follow different paths through the program. How?
- Code at different UEs can differentiate with each other using a unique ID.
- Assumes that each underlying hardware are similar.

Challenges

- Interactions among the seemingly independent activities of UEs.
- Clarity, Scalability, Efficiency, Maintainability (1m cores), Environment.
- How to handle code like initialization, finalization etc?

Supporting structures

- We have identified concurrency, and established an algorithm structure.
- Now how to implement the algorithm?

Issues

- Clarity of abstraction from algorithm to source code.
- Scalability how many processors can it use?
- Efficiency utilizing the resource of the computer, *efficiently*. Example?
- Maintainability is it easy to debug, verify and modify?
- Environment hardware and programming environment.



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SPMD example

$$\pi = \int_0^1 \frac{4}{1+x^x} \mathrm{d}x$$

int main () { Initialization start 11 int i; int numSteps = 1000000;double x, pi, step, sum = 0.0; step = 1.0/(double) numSteps; // Initialization end for (i=0;i< numSteps; i++) {</pre> x = (i+0.5) * step;sum = sum + 4.0/(1.0+x*x); } // Finalization start pi = step * sum; printf("pi %lf\n",pi); return 0; // Finalization end

SPMD translation. Inefficient?

int main () {

```
int i;
int numSteps = 1000000;
double x, pi, step, sum = 0.0;
step = 1.0/(double) numSteps;
int numProcs = numSteps;
int myID = getMyId();
```

i = myID; x = (i+0.5)*step; sum = sum + 4.0/(1.0+x*x);

sum = step * sum;

DoReductionOverAllProcs(&sum, &pi); // blocking.

if (myID == 0) printf("pi %lf\n",pi);
return 0;

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Supporting structure





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SPMD translation. Better?

int main () {

int i; int numSteps = 1000000; double x, pi, step, sum = 0.0; step = 1.0/(double) numSteps; int numProcs = getNumProcs(); int myID = getMyId(); step = 1.0/numSteps;

iStart = myID * (numSteps / numprocs); iEnd = iStart * (numSteps / numprocs); if (myID == numProcs-1) iEnd = numSteps;

for (i = iStart; i < iEnd; ++i) {

x = (i+0.5)*step; sum = sum + 4.0/(1.0+x*x); } sum = step * sum; DoReductionOverAllProcs(&sum, &pi); // blocking. if (myID == 0) printf("pi %lf\n",pi); return 0; } VKrishna Nandivada (IIT Madras) CS6868 (IIT Madras)

Master/Worker

Situation

- workload at each task is variable and unpredictable (what if predictable?).
- Not easy to map to loop-based computation.
- The underlying hardware have different capacities.

Master/Worker pattern

- Has a logical master, and one or more instances of workers.
- Computation by each worker may vary.
- The master starts computation and creates a set of tasks.
- Master waits for tasks to get over.

Master/Worker layout



Master/Worker template for master

int nTasks // Number of tasks int nWorkers // Number of workers public static SharedQueue taskQueue; // global task queue public static SharedQueue resultsQueue; // queue to hold result: void master() { // Create and initialize shared data structures taskQueue = new SharedQueue(); globalResults = new SharedQueue(); for (int i = 0; i < nTasks; i++) enqueue(taskQueue, i); } // Create and key thready

```
// Create nWorkers threads
ForkJoin (nWorkers);
```

```
consumeResults (nTasks);
```

```
}
```

Master/Worker Issues

- Has good scalability, if number of tasks greatly exceed the number of workers, and each worker roughly gets the same amount of work (Why?).
- Size of tasks should not be too small. Why?
- Can work with any hardware platform.
- How to detect completion? When can the workers not wait but shutdown?
 - Easy if all tasks are ready before workers start.
 - Use of a poison-pill in the work-queue.
 - What if the workers can also add tasks? Issues?
 - Issues with asynchronous message passing systems?
 - How to handle fault tolerance? did the task finish?

Variations

- Master can also become a worker.
- Distributed task queue instead of a centralized task queue. (dis)advantages?

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Master/Worker - ForkJoin



Master/Worker - template for worker

- "Map" step: The master node takes the input, partitions it up into smaller sub-problems, and distributes those to worker nodes.
 - A worker may again partition the problem multi-level tree structure.
 - The worker node processes that smaller problem, and passes the answer back to its master node.
- "Reduce" step: Master node takes all the answers and combines them to get the output the answer to the original problem.

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Loop Parallelization

- A program has many computationally intensive loops, with "independent" iterations.
- Goal: Parallelize the loops and get most of the benefits.
- Very narrow focus.
- Typical application: scientific and high performance computation.
- Impact of Amdahl's law?
- Quite amenable to refactoring type of incremental parallelization. Advantage?
- Impact on distributed memory systems?
- Good if computation done in iterations compensates the cost of thread creation - how to improve the tradeoff? Coalescing, merging.

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Supporting structure



Loop coalescing and merging for parallelization

Merging/Fusion

Coalescing for (i : 1..n) { for (i : 0..m) { S1 for (j : 0..n) { S for (j : 1..n) { S2 --> for (ij : 0..m*n) { --> j = ij % n;for (i : 1..n) { i = ij / n;S1 S j = i; S2

Loop parallelization issues

- Distributed memory architectures.
- False sharing : variables not needed to be shared, but are in the same same cache line. Can incur high overheads.
- Seen in systems with distributed, coherent caches.
- The caching protocol may force the reload of a cache line despite a lack of logical necessity.



Supporting structure





$$\pi = \int_0^1 \frac{4}{1+x^x} \mathrm{d}x$$

int main () {

<pre>int i,numSteps = 1000000; double x,pi,step,sum=0.0; step=1.0/(double)numSteps</pre>	<pre>int i,numSteps=1000000; double pi,step,sum=0.0; step=1.0/(double)numSteps;</pre>
<pre>for(i: [0numSteps]){ x=(i+0.5)*step; sum=sum+4.0/(1.0+x*x);}</pre>	<pre>forall(i: [0numSteps]){ double x=(i+0.5)*step; double tmp=4.0/(1.0+x*x) atomic sum=sum+tmp; }</pre>
<pre>pi=step*sum; printf("pi %lf\n",pi); return 0; } eading material: Automatic loop pa</pre>	<pre>pi = step * sum; printf("pi %lf\n",pi); return 0; } arallelization.</pre>
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Fork/Join

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int main () {

- The number of concurrent tasks varies as the program executes.
- Parallelism beyond just loops.
- Tasks created dynamically (beyond master-worker).
- One or more tasks waits for the created tasks to terminate.
- Each task may or not result in an actual UE. Many-to-one mapping. Examples?



int[] mergesort(int[]A, int L, int H) { if $(H-L \leq T)$ {quickSort(A, L, H); return; } int m = (L+H)/2;A1 = mergesort (A, L, m); // fork A2 = mergesort (A, m+1, H); // fork // join. return merge(A1, A2); // returns a merged sorted array.

Issues

- Cost.
- Alternatives?



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Supporting structure



Supporting structures and algorithm structure

	Task Parallelism	Divide and Conquer	Geometric Decomposition	Recursive Data	Pipeline	Event- Based Coordination
SPMD	****	***	****	**	***	**
Loop Parallelism	****	**	***			-
Master/ Worker	****	**	*	*	*	*
Fork/Join	**	****	**		****	****

Homework

	OpenMP	MPI	Java	X10	UPC	Cilk	Hadoop
SPMD	***	****	**				
Loop Parallelism	****	*	***				
Master/Worker	**	***	***				
Fork/Join	***		****				

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Shared Data

Million dollar question: How to handle shared data?

- Managing shared data incurs overhead.
- Scalability can become an issue.
- Can lead to programmability issues.
- Avoid if possible by
 - replication,
 - privatization,
 - reduction.
- Use appropriate concurrency control. Why?
 - Should preserve the semantics.
 - Should not be too conservative.
- Shared data organization: distributed or at a central location?
- Shared Queue (remember master-worker?) is a type of shared data.

Issues with shared data

 Data race and interference: Two shared activities access a shared data. And at least one of them is a write. The activities said to interfere.

```
forall (i:[1..n]) {
  sum += A[i];
for (i[1..n]) {
forall (j=1; j<m; ++j) {</pre>
   A[i][j] = (A[i-1][j-1] + A[i-1][j] + A[i-1][j+1])/3;
```

• Dependencies : Use synchronization (locks, barriers, atomics, ...) to enforce the dependencies.

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• How to implement all-to-all synchronization?

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Supporting structure



Issues with shared data

Deadlocks : two or more competing actions are each waiting for the other to finish.

 $lockA \rightarrow lockB$ (Example via nested locks) = $lockB \rightarrow lockA$

One way to avoid: partial order among locks. Locks are acquired in an order respecting the partial order.

- Livelocks : the states of the processes involved in the livelock constantly change with regard to one another, none progressing. Example: recovery from deadlock - If more than one process takes action, the deadlock detection algorithm can be repeatedly triggered leading to a livelock
- Locality : Trivial if data is not shared.
- Memory synchronization: when memory / cache is distributed.
- Task scheduling tasks might be suspended for access to shared data. Minimize the wait.

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Distributed Array

Arrays often are partitioned between multiple tasks. Goal: Efficient code, programmability.

- Distribute the arrays such that elelement needed by a task is "available" and "nearby".
- Array element redistribution?
- An abstraction is needed: a map from elements to places.
- Some standard ones: Blocked, Cyclic, Blocked cyclic, Unique,
- Chosing a distribution.







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UE management

- UE unit of execution (a process / thread / activity)
- Difference between process / thread / activity.
- Management = Creation, execution, termination.
- Varies with different underlying languages.
- Go back to first few lectures for a recap.

Synchronization: Memory synchronization and fences

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done=true;

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while(done) ;

- done = false;
- Value may be present in cache. cache coherence may take care.
- Value may be present in a register Culprit compiler.
- Value may not be read. How?

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	$\mathbf{x} = \mathbf{y} = 0$
Thread 1	Thread 2
1: r1 = x	4: x = 1
2: y = 1	r3 = y
3: r2 = x	
r1 == r2 ==	= r3 == 0. Possible?



- A memory fences guarantees that the UEs will see a consistent view of memory.
- Writes performed before the fence will be visible to reads performed after the fence.
- Reads performed after the fence will obtain a value written no earlier than the latest write before the fence.
- Only for shared memory.
- Explicit management can be error prone. High level: OpenMP flush, shared, Java volatile. *Read yourself.*

Barrier is a synchronization point at which every member of a collection of UEs must arrive before any member can proceed.

- MPI_Barrier, join, finish, clocks, phasers
- Implemented underneath via passing messages.





- Barriers
- Mutual exclusion: Java synchronized, omp_set_lock, omp_unset_lock.





Communication

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Collective communication

- UEs need to exchange information.
 - Shared memory easy. Challenge synchronize the memory access so that results are correct irrespective of scheduling.
 - distributed memory not much need for synchronization to protect the resources. → Communication plays a big role.
- One to one communication :
- Between all UEs in one event: Collective communication.

When multiple UEs participate in a single communication event, the event is called a collective communication operation. Examples:

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- Broadcast: a mechanism to send single message to all UEs.
- Barriers : a synchronization point.
- Reduction: Take a collection of objects, one from each UE, and "combine" into a single value;
 - combined value present only on one UE?
 - combined value present on all UEs?



Serial reduction



- Reduction with *n* items takes *n* steps.
- Useful especially if the reduction operator is not associative.
- Only one UE knows the result.

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Recursive doubling



- Reduction with $2 \times n$ items takes *n* steps.
- What if number of UEs < number of data items?
- All UEs know the result.



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Tree based reduction



- Reduction with 2^n items takes *n* steps.
- What if number of UEs < number of data items?
- Only one UE knows the result.
- Associative + Commutative or don't care (example?)

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Implementation Mechanisms





Overall big picture



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