CS3300 - Compiler Design

Liveness analysis and Register allocation

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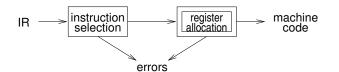
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Register allocation



Register allocation:

- have value in a register when used
- limited resources
- can effect the instruction choices
- can move loads and stores
- optimal allocation is difficult
 - \Rightarrow NP-complete for $k \ge 1$ registers

Liveness analysis

Problem:

- IR contains an unbounded number of temporaries
- machine has bounded number of registers

Approach:

- temporaries with disjoint live ranges can map to same register
- if not enough registers then <u>spill</u> some temporaries (i.e., keep them in memory)
- The compiler must perform liveness analysis for each temporary:

It is <u>live</u> if it holds a value that may be needed in future



 $a \leftarrow 0$ $L_1: \quad b \leftarrow a+1$ $c \leftarrow c+b$ $a \leftarrow b \times 2$ if a < N goto L_1 return c

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Definitions

- v is live on edge e if there is a directed path from e to a use of v that does not pass through any def(v)
- v is live-in at node n if live on any of n's in-edges
- v is live-out at n if live on any of n's out-edges
- $v \in USE[n] \Rightarrow v$ live-in at n
- (For programs with statically established no uninitialized variables)
 v live-in at *n* ⇒ *v* live-out at all *m* ∈ *pred*[*n*]
- *v* live-out at $n, v \notin def[n] \Rightarrow v$ live-in at n

Gathering liveness information is a form of <u>data flow analysis</u> operating over the CFG:

- We will treat each statement as a different basic block.
- liveness of variables "flows" around the edges of the graph
- assignments define a variable, v:
 - def(v) = set of graph nodes that define v
 - def[n] = set of variables defined by n
- occurrences of v in expressions use it:
 - USE(v) = set of nodes that use v
 - *USE*[*n*] = set of variables used in *n*



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Liveness analysis

Define:

```
in[n] = variables live-in at n
out[n] = variables live-out at n
```

Then:

$$out[n] = \bigcup_{s \in succ(n)} in[s]$$

 $succ[n] = \phi \Rightarrow out[n] = \phi$

Note:

 $in[n] \supseteq use[n]$ $in[n] \supseteq out[n] - def[n]$

use[n] and def[n] are constant (independent of control flow) Now, $v \in in[n]$ iff. $v \in use[n]$ or $v \in out[n] - def[n]$ Thus, $in[n] = use[n] \cup (out[n] - def[n])$ VKrishna Nandivada (IIT Madras)



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N: Set of nodes of CFG;foreach $\underline{n \in N}$ do $| in[n] \leftarrow \phi;$ $out[n] \leftarrow \phi;$ end repeat foreach $\underline{n \in \text{Nodes}}$ do $| in'[n] \leftarrow in[n];$ $out'[n] \leftarrow out[n];$ $in[n] \leftarrow use[n] \cup (out[n] - def[n]);$ $out[n] \leftarrow \bigcup_{s \in succ[n]} in[s];$ end until $\forall n, in'[n] = in[n] \land out'[n] = out[n];$

Notes

- should order computation of inner loop to follow the "flow"
- liveness flows backward along control-flow arcs, from out to in
- nodes can just as easily be basic blocks to reduce CFG size
- could do one variable at a time, from <u>uses</u> back to <u>defs</u>, noting liveness along the way

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Iterative solution for liveness

Complexity: for input program of size N

- $\leq N$ nodes in CFG
 - $\Rightarrow \leq N$ variables
 - \Rightarrow N elements per *in/out*
 - \Rightarrow O(N) time per set-union
- for loop performs constant number of set operations per node $\Rightarrow O(N^2)$ time for for loop
- each iteration of **repeat** loop can only add to each set sets can contain at most every variable
 - \Rightarrow sizes of all in and out sets sum to $2N^2$,
 - bounding the number of iterations of the repeat loop
- \Rightarrow worst-case complexity of O(N^4)
- ordering can cut **repeat** loop down to 2-3 iterations $\Rightarrow O(N)$ or $O(N^2)$ in practice



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Least fixed points

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There is often more than one solution for a given dataflow problem (see example).

Any solution to dataflow equations is a conservative approximation:

• v has some later use downstream from n

 $\Rightarrow v \in out(n)$

• but not the converse

Conservatively assuming a variable is live does not break the program; just means more registers may be needed.

Assuming a variable is dead when really live will break things.

Many possible solutions but we want the "smallest": the least fixpoint. The iterative algorithm computes this least fixpoint.



• Step 1:

- Select target machine instructions assuming infinite registers (temps).
- If a instruction requires a special register replace that temp with that register.
- Step 2:
 - Construct an interference graph.
 - Solve the register allocation problem by coloring the graph.
 - A graph is said to be <u>colored</u> if each each pair of neighboring nodes have different colors.

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Example 1, available colors = 2

Graph coloring - a simplistic approach

Input: *G* - the interference graph, *K* - number of colors **repeat**

repeat

- Remove a node n and all its edges from G, such that degree of n is less than K;
- Push *n* onto a stack;

until <u>G</u> has no node with degree less than K;

// G is either empty or all of its nodes have degree \geq K

if G is not empty then

- Take one node *m* out of *G*, and mark it for spilling;
- Remove all the edges of m from G;

end

until G is empty;

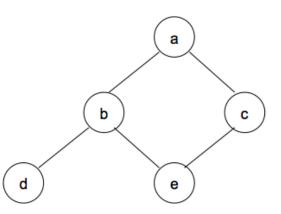
Take one node at a time from the stack and assign a <u>non conflicting</u> color.



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Example 2



We have to spill.

Graph coloring - Kempe's heuristic

• Algorithm dating back to 1879.

Input: *G* - the interference graph, *K* - number of colors **repeat**

repeat

Remove a node n and all its edges from G, such that degree of n is less than K;

Push *n* onto a stack;

until <u>G has no node with degree less than K;</u>

// G is either empty or all of its nodes have degree \geq K

if G is not empty then

Take one node m out of G.;

push *m* onto the stack;

end

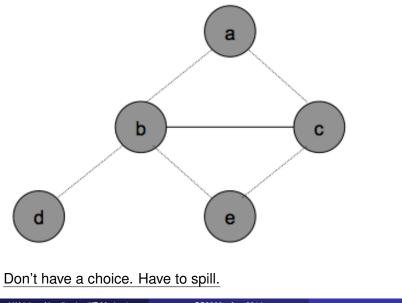
until G is empty;

Take one node at a time from the stack and assign a non conflicting color (1) possible, else spill).

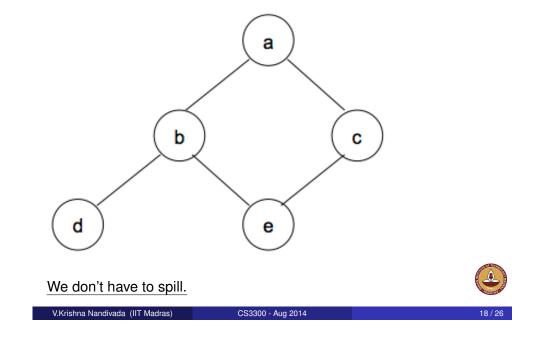
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Example 3



Example 2 (revisited)



Register allocation - Linear scan

Register allocation is **expensive**.

- Many algorithms use heuristics for graph coloring.
- Allocation may take time quadratic in the number of live intervals.

Not suitable

- Online compilers need to generate code quickly. e.g. JIT compilers.
- Sacrifice efficient register allocation for compilation speed.

Linear scan register allocation - Massimiliano Poletto and Vivek Sarkar, ACM TOPLAS 1999



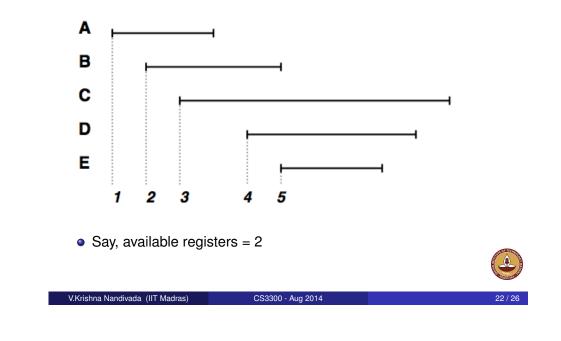
Linear Scan algorithm

LINEARSCANREGISTERALLOCATION	
active $\leftarrow \{\}$	
for each live interval i , in order of increasing start point	
$\operatorname{ExpireOldIntervals}(i)$	
$\mathbf{if} \operatorname{length}(active) = R \mathbf{then}$	
${ m SpillAtInterval}(i)$	
else	
$register[i] \leftarrow a register removed from pool of free registers$	
add i to active, sorted by increasing end point	
ExpireOldIntervals(i)	
foreach interval <i>i</i> in <i>active</i> , in order of increasing end point	
if $endpoint[j] \geq startpoint[i]$ then	
return	
remove i from <i>active</i>	
add $register[j]$ to pool of free registers	
$\operatorname{SpillAtInterval}(i)$	
$spill \leftarrow last interval in active$	
if $endpoint[spill] > endpoint[i]$ then	
$register[i] \leftarrow register[spill]$	
$location[spill] \leftarrow$ new stack location	
remove spill from active	
add i to active, sorted by increasing end point	STREET STREET
else	
$location[i] \leftarrow$ new stack location	Station of a state
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Linear Scan algorithm - analysis

- Each live range gets either a register or a spill location.
- Note: The number of overlapping intervals changes only at the start and end points of an interval.
- Live intervals are stored in a list that is sorted in order of increasing start point.
- The <u>active</u> list is kept sorted in order of increasing end point. Adv: need to scan only those intervals (+1 at most) that have to be removed.
- Complexity: O(V) if number of registers is assumed ot be a constant. Else? O(V × logR)

Example



Spilling

- We need to generate extra instructions to load variables from the stack and store them back.
- The load and store may require registers again:
 - Naive approach: Keep a separate register (wasteful).
 - Rewrite the code by introducing a temporary; rerun the liveness + ra.

(Note: the new temp has much smaller live range).



Consider: add t1 t2

- Suppose t2 has to be spilled, say to [sp-4].
- Invent a new temp t35, and rewrite:

```
mov t35 [sp-4]
add t1 t35
```

- t35 has a very short live range and less likely to interfere.
- Now rerun the algo.

Criteria for spilling

During register allocation, we identify that one of the live ranges from a given set, has to be spilled. Criteria?

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- Random! Adv? Disadv?
- One with maximum degree
- One that has the longest life
- One with the shortest life (take advantage of the cache).
- One with least cost.

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- Cost = Dynamic (load cost + store cost)
- How to handle loops, conditionals?
- Cost of load, store





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