

CS6848 - Principles of Programming Languages

Principles of Programming Languages

V. Krishna Nandivada

IIT Madras

Recall

$e ::= x \mid \lambda x.e \mid e_1 e_2 \mid c \mid \text{succ } e$
 $x \in \text{Identifier (infinite set of variables)}$
 $c \in \text{Integer}$
 $v ::= c \mid \lambda x.e$
 $t ::= \text{Int} \mid t \rightarrow t$



Recap

- Structural subtyping
- Unification algorithm



Extending a language

- Extend the language grammar that will lead to new terms.
- Extend the allowed values.
- Extend the types.
- New operational semantics.
- New typing rules.



Pairs

- Expressions

$$e ::= \dots | (e_1, e_2) | e.1 | e.2$$

- Values

$$v ::= \dots | (v_1, v_2)$$

- Types

$$t ::= \dots | t_1 \times t_2$$



New operational semantics

- First element:

$$(Pair \beta 1) \quad (v_1, v_2).1 \rightarrow v_1$$

- Second element:

$$(Pair \beta 2) \quad (v_1, v_2).2 \rightarrow v_2$$

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$$\text{Projection 1} \quad \frac{e \rightarrow e'}{e.1 \rightarrow e'.1}$$

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$$\text{Projection 2} \quad \frac{e \rightarrow e'}{e.2 \rightarrow e'.2}$$

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$$\text{Pair Evaluation 1} \quad \frac{e_1 \rightarrow e'_1}{(e_1, e_2) \rightarrow (e'_1, e_2)}$$

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$$\text{Pair Evaluation 2} \quad \frac{e_2 \rightarrow e'_2}{(v_1, e_2) \rightarrow (v_1, e'_2)}$$



Typing rules for pairs

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$$\text{Pair} \quad \frac{A \vdash e_1 : t_1 \quad A \vdash e_2 : t_2}{A \vdash (e_1, e_2) : t_1 \times t_2}$$

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$$\text{Projection 1} \quad \frac{A \vdash e : t_1 \times t_2}{A \vdash e.1 : t_1}$$

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$$\text{Projection 2} \quad \frac{A \vdash e : t_1 \times t_2}{A \vdash e.2 : t_2}$$



Properties of pairs

- The components are evaluated left to right.
- The pair must be fully evaluated to get the components.
- A pair that is passed as an argument will be fully evaluated, before the function starts executing (in call by value semantics).



- Expressions

$$e ::= \dots | (e_i^{i \in 1..n}) | e.i$$

- Values

$$v ::= \dots | (v_i^{i \in 1..n})$$

- Types

$$t ::= \dots | (t_i^{i \in 1..n})$$



- Element j :

$$(\beta)(v_i^{i \in 1..n}).j \rightarrow v_j$$

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$$\text{Projection 1} \frac{e \rightarrow e'}{e.i \rightarrow e'.i}$$

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$$\text{Tuple Evaluation} \frac{e_j \rightarrow e'_j}{(v_i^{i \in 1..j-1}, e_j, e_k^{k \in j+1..n}) \rightarrow (v_i^{i \in 1..j-1}, e'_j, e_k^{k \in j+1..n})}$$



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$$\text{Tuple} \frac{A \vdash \forall i e_i : t_i}{A \vdash (e_i^{i \in 1..n}) : (t_i^{i \in 1..n})}$$

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$$\text{Projection} \frac{A \vdash e : (t_i^{i \in 1..n})}{A \vdash e.j : t_j}$$



- Expressions

$$e ::= \dots | (l_i = e_i^{i \in 1..n}) | e.l$$

- Values

$$v ::= \dots | (l_i = v_i^{i \in 1..n})$$

- Types

$$t ::= \dots | (l_i : t_i^{i \in 1..n})$$



- Element j :

β reduction $(l_i : v_i^{i \in 1..n}).l_j \rightarrow v_j$

Projection 1 $\frac{e \rightarrow e'}{e.l \rightarrow e'.l}$

Record Evaluation $\frac{e_j \rightarrow e'_j}{(l_i = v_i^{i \in 1..j-1}, l_j = e_j, l_k = e_k^{k \in j+1..n}) \rightarrow (l_i = v_i^{i \in 1..j-1}, l_j = e'_j, l_k = e_k^{k \in j+1..n})}$



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Tuple $\frac{A \vdash \forall i e_i : t_i}{A \vdash (l_i = e_i^{i \in 1..n}) : (l_i : t_i^{i \in 1..n})}$

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Projection $\frac{A \vdash e : (l_i : t_i^{i \in 1..n})}{A \vdash e.l_j : t_j}$

