

# Pointer Analysis

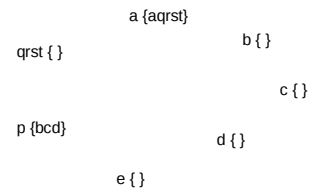
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CS6843 Program Analysis  
IIT Madras  
Jan 2016

## Points-to Analysis as a Graph Problem

$*e = c, c = *a, e = d, b = a, *a = p$

Initially,  $a \rightarrow \{a, q, r, s, t\}, p \rightarrow \{b, c, d\}$



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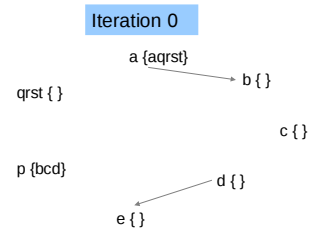
## Outline

- Introduction
- Pointer analysis as a DFA problem
- Design decisions
- Andersen's analysis, Steensgaard's analysis
- Pointer analysis as a graph problem
  - Optimizations
- Pointer analysis as graph rewrite rules
- Applications
- Parallelization
  - Constraint based
  - Replication based

## Points-to Analysis as a Graph Problem

$*e = c, c = *a, e = d, b = a, *a = p$

Initially,  $a \rightarrow \{a, q, r, s, t\}, p \rightarrow \{b, c, d\}$



$e = d$   
 $b = a$   
-----  
 $*e = c$   
 $c = *a$   
 $*a = p$

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## Points-to Analysis as a Graph Problem

Each pointer as a node, directed edge  $q \rightarrow p$  indicates points-to set of  $q$  is a subset of that of  $p$ .

**Input:** set  $C$  of points-to constraints

Process address-of constraints

Add edges to constraint graph  $G$  using copy constraints

repeat

Propagate points-to information in  $G$

Add edges to  $G$  using load and store constraints

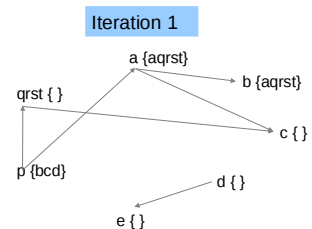
until fixpoint

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## Points-to Analysis as a Graph Problem

$*e = c, c = *a, e = d, b = a, *a = p$

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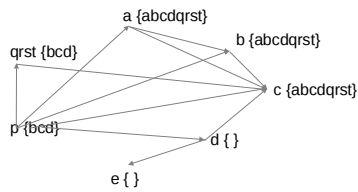
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## Points-to Analysis as a Graph Problem

\*e = c, c = \*a, e = d, b = a, \*a = p

Initially, a → {a,q,r,s,t}, p → {b,c,d}

Iteration 2



e = d  
b = a  
-----  
\*e = c  
c = \*a  
\*a = p

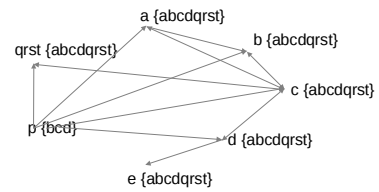
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## Points-to Analysis as a Graph Problem

\*e = c, c = \*a, e = d, b = a, \*a = p

Initially, a → {a,q,r,s,t}, p → {b,c,d}

Iteration 5: fixed-point



e = d  
b = a  
-----  
\*e = c  
c = \*a  
\*a = p

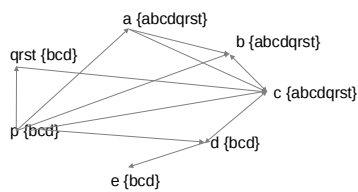
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## Points-to Analysis as a Graph Problem

\*e = c, c = \*a, e = d, b = a, \*a = p

Initially, a → {a,q,r,s,t}, p → {b,c,d}

Iteration 3



e = d  
b = a  
-----  
\*e = c  
c = \*a  
\*a = p

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## Why a Graph Formulation?

- A naïve formulation offers no benefits over the constraint-based formulation.
- We need to exploit structural properties of the constraint graph for efficient execution.
  - Online cycle detection
  - Online dominator detection
  - Propagation order: Topological sort, Depth first

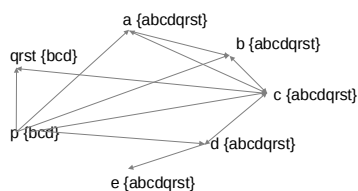
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## Points-to Analysis as a Graph Problem

\*e = c, c = \*a, e = d, b = a, \*a = p

Initially, a → {a,q,r,s,t}, p → {b,c,d}

Iteration 4



e = d  
b = a  
-----  
\*e = c  
c = \*a  
\*a = p


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## Pointer Equivalence

- Two pointers are equivalent if they have the same points-to sets. Simple.
- If we identify such pointers *before* computing their points-to information, we can reduce the number of pointers tracked during the analysis.
- Now let's go back to the constraint graph.

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## Why a Graph Formulation?

- If the program contains statements  $a = b$ ,  $b = a$ , what can you say about the points-to sets of  $a$  and  $b$  at the fixed-point?
- How does the constraint graph look like? 
- How about  $a = b$ ,  $b = c$ ,  $c = a$ ?
- How about  $a = c$ ,  $b = *p$ ,  $c = b$ ?

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## Offline Variable Substitution

- But some constraints were easy to check for equivalence without running the analysis.
  - $a = b$ ,  $b = a$
  - $a = *p$ ,  $*p = a$
  - $a = b$ ,  $c = a$ ,  $c = b$  and no other incoming edge to  $c$ .
- OVS is performed before running pointer analysis.

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## Online Cycle Detection

- Edges get added to the graph dynamically.
- So, cycle detection is performed online.
- Cycles are collapsed – usually replaced with a representative.
- Can use union-find.

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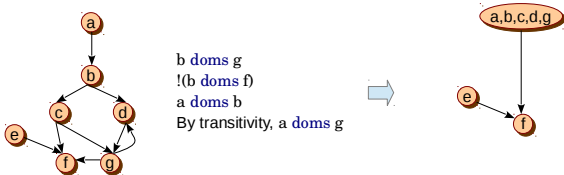
## Propagation Order

- A topological ordering is beneficial for propagating points-to information (wave propagation)
- The information may also be propagated in depth-first manner (deep propagation)
- DP is helpful to reuse the difference in points-to information

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## Online Dominator Detection

- If two nodes in a constraint graph have the same dominator, they are pointer equivalent.
- A dominator and its dominees are pointer equivalent.
- **doms** is a transitive relation.



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## How About Constraint Order?

- Given a set of constraints, find an optimal way of evaluating them
- Like most CS problems, this is NP-Complete
- Reducible from Set Cover

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## Reduction from Set Cover

- Given an instance of Set Cover  $SC(U, S, K)$

- $U$ : universe of elements
- $S$ : set of subsets  $S_i$
- $K$ : some number

$S = \{1, 4\}, \{2, 5\}, \{2, 4, 5\}, \{3\}$   
 Solution Two:  $\{1, 4\}, \{2, 4, 5\}, \{3\}$   
 Solution One:  $\{1, 4\}, \{2, 5\}, \{3\}$

whether there exists a set of  $K$  subsets covering  $U$

- Reduce to  $PTA(C, S, K)$  where
  - $C$  is a set of copy constraints
  - $S$  is a variable of interest w.r.t. fixed-point
  - $K$  is the number of steps in which the fixed-point is reached

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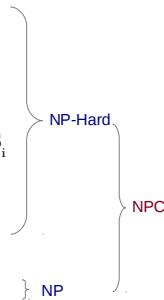
## Constraint Priority

- Priority of a constraint in iteration  $i$  is the amount of **new points-to information** it adds in iteration  $(i - 1)$ .
- Constraints are **grouped** in different priority levels which are ordered based on their priority.
- A constraint may **jump** across multiple priority levels during the analysis.

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## $SC \geq PTA$

- $SC(U, S, K) \geq PTA(C, S, K)$
- Linear time reduction
  - for each  $s \in S_i$  add  $s$  to  $ptsto(S_i)$
  - for each set  $S_i$  create a copy statement  $S = S_i$
- A solution to  $PTA \Rightarrow$  A solution to  $SC$
- A solution to  $PTA \Leftarrow$  A solution to  $SC$
- Poly-time verification



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## Bucketization



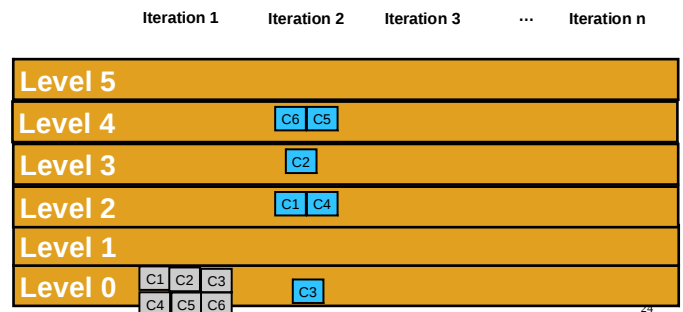
## How About Constraint Order?

- Given a set of constraints, find an optimal way of evaluating them
- Like most CS problems, this is NP-Complete
- Reducible from Set Cover
- Need to depend upon heuristics

What would be a good heuristic?

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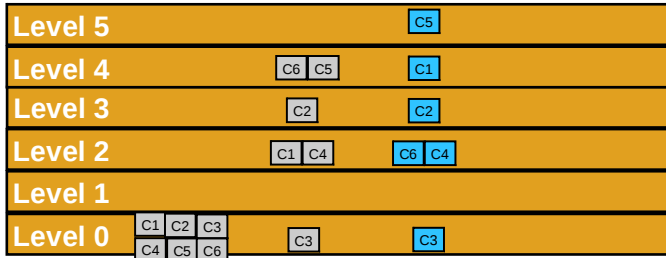
## Bucketization



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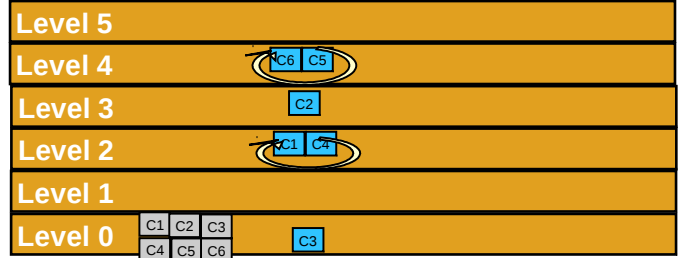
## Bucketization

Iteration 1    Iteration 2    Iteration 3    ...    Iteration n



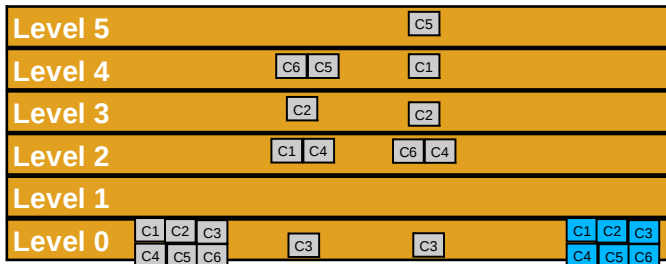
## Skewed Evaluation

Iteration 1    Iteration 2    Iteration 3    ...    Iteration n



## Bucketization

Iteration 1    Iteration 2    Iteration 3    ...    Iteration n



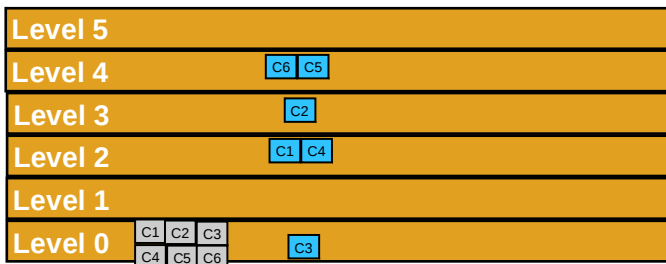
## Prioritized Points-to Analysis

Processing order

\*a = p (18)  
c = \*a (8)  
\*e = c (0)

## Skewed Evaluation

Iteration 1    Iteration 2    Iteration 3    ...    Iteration n

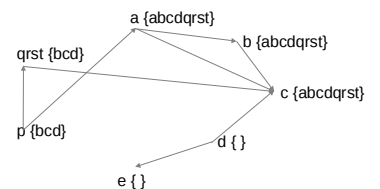


## Prioritized Points-to Analysis

Processing order

\*a = p (18)  
c = \*a (8)  
\*e = c (0)

Priority: Iteration 1



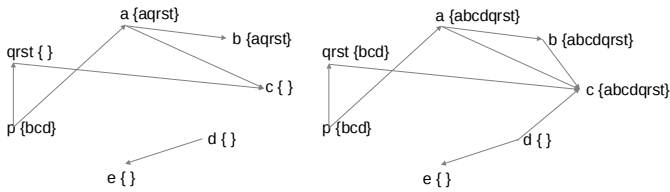
## Prioritized Points-to Analysis

Fixed Processing order  
 $*e = c$   
 $c = *a$   
 $*a = p$

Andersen: Iteration 1

Processing order  
 $*a = p$  (18)  
 $c = *a$  (8)  
 $*e = c$  (0)

Priority: Iteration 1



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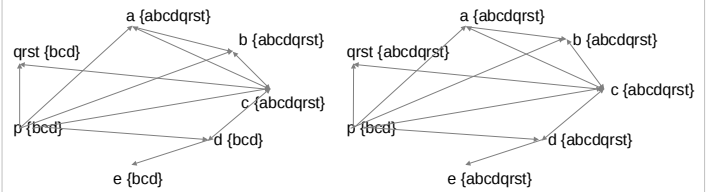
## Prioritized Points-to Analysis

Fixed Processing order  
 $*e = c$   
 $c = *a$   
 $*a = p$

Andersen: Iteration 4

Processing order  
 $*e = c$  (0)  
 $*a = p$  (0)  
 $c = *a$  (0)

Priority: fixed-point



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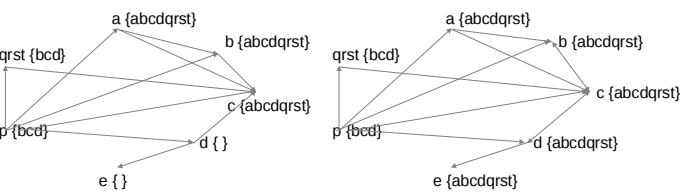
## Prioritized Points-to Analysis

Fixed Processing order  
 $*e = c$   
 $c = *a$   
 $*a = p$

Andersen: Iteration 2

Processing order  
 $*a = p$  (6)  
 $c = *a$  (0)  
 $*e = c$  (10)

Priority: Iteration 2



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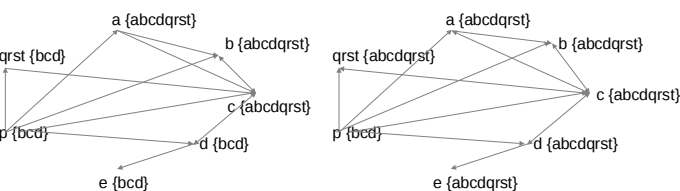
## Prioritized Points-to Analysis

Fixed Processing order  
 $*e = c$   
 $c = *a$   
 $*a = p$

Andersen: Iteration 3

Processing order  
 $*e = c$  (20)  
 $*a = p$  (0)  
 $c = *a$  (0)

Priority: Iteration 3



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