Parallelization

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Control Dependence

• if (x == 4) y = 10; else y = 1;

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Speedup

- Speedup = Ts / Tp
- Amdahl's Law: Speedup is limited by the sequential part of the task.
- If 20% of the task is sequential, program's speedup is limited to 5 (irrespective of the number of cores or amount of effort).

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Data Dependence

- pi = 3.142; r = 5.0; area = pi * r * r;
- Types
 - True / Flow / RAW: S1 δ S2 (x = ...; ... = x;)
 - Anti / WAR: S1 δ^{-1} S2 (... = x; x = ...)
 - Output / WAW: S1 δ^{o} S2 (x = ...; x = ...)

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Instruction Parallel vs. Data Parallel

- Parallelism extracted from multiple instructions on the data items.
- Parallelism extracted from the same task on different data items.







S1 is the source and S3 is the sink of the dependence.

Program Order vs. Dependence

- Sequential order imposed by the program is too restrictive.
- Only the partial order of all dependences need to be maintained by the compiler to guarantee program correctness.
- So, reorder flow; maintain dependence.

Advantages of Reordering

- · Improved locality
 - Spatial: matrix operations
 - Temporal: xinit(); yinit(); xcompute(); ycompute();
- · Improved load balance
 - small1(); big1(); small2(); big2();
- Improved parallelism
 - xuse(); xdef(); yuse(); ydef();

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Reordering Transformations

- A reordering transformation is any program transformation that merely changes the execution order of the code, without adding or deleting any executions of any statements.
- A reordering transformation preserves a dependence if it preserves the relative execution order of the source and the sink of that dependence.
- Theorem: Any reordering transformation that preserves every dependence in a program leads to an equivalent computation.

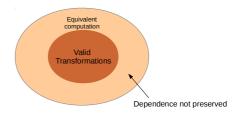
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Let's Focus on Loops

- Iteration vector: Sequence of outer loops.
 - iv = (ioutermost, ..., imiddle, ..., iinnermost)
 - For instance (i, j, k).
- Iteration space: Set of all possible iteration vectors for a statement.
- Statement instance: S(i)
- S(i) δ S(j) iff
 - (a) i < j or (i == j and $S1 \Rightarrow \Rightarrow S2$ path in loop-body)
 - (b) both access the same memory location
 - (c) at least one of the accesses is a write

Valid Transformations

 A transformation is valid for the program to which it applies if it preserves all the dependences in the program.



Classwork: Write a simple transformation that maintains computation equivalence but does not preserve dependence.

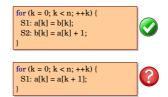
Safe Transformations

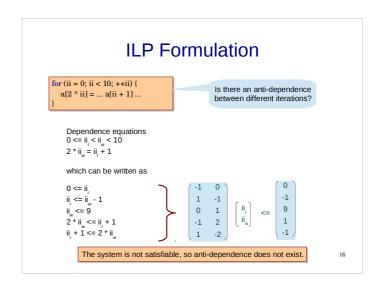
Loop Dependence Theorem

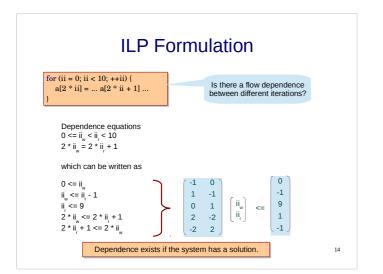
- There exists a dependence from statement S1 to statement S2 in a common nest of loops iff there exist two iteration vectors i and j for the nest, such that S1(i) δ S2(j).
- Two computations are equivalent if on the same inputs they produce the same output.
- A transformation is safe if it leads to an equivalent program.

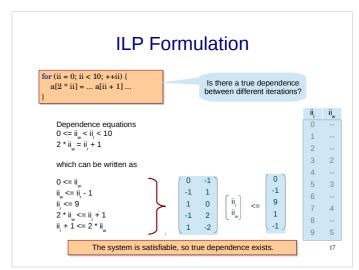
Loop Parallelization

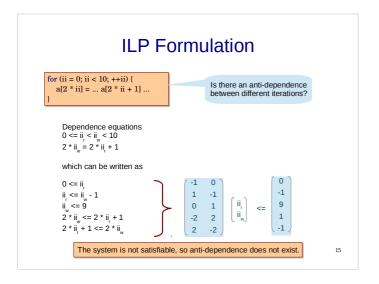
 Theorem: It is valid to convert a sequential loop to a parallel loop if the loop carries no dependence.

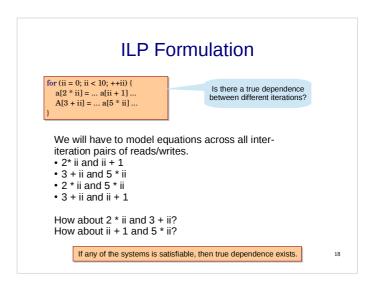












Managing Races

- Data-race between iterations p and q for element a[f(i)].
- · Critical section
 - Locks
 - Atomics
 - Barriers

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Inserting Locks

• Sometimes, a lock may be for a simple operation

```
if (i == p | | i == q) {
    lock(f(i));
    sum += a[i];
    unlock(f(i));
}
```

 A simple critical section may be convertible to atomics.

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Inserting Locks

 Data-race between iterations p and q for element a[f(i)].

```
if (i == p | | i == q) {
    lock(f(i));
    ... perform operation ... 
    unlock(f(i));
}
This operation could be same or different for the involved threads.
```

· e.g., Producer-consumer

```
produce() {
    while (...) {
        items.add(...);
    }
}
consume() {
    e = items.remove();
}
```

Inserting Atomics

- If the operation is simple
 - Primitive type
 - Single element
 - Relative update / read-write
- Example
 - Producer-consumer with single element update
- Types
 - increment, decrement
 - add, sub
 - min, max
 - exch, CAS

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Inserting Locks

- For multiple data items a[f(i)] and a[g(i)]
 - Single lock
 - Multiple locks
- Multiple locks may lead to deadlock
 - may allow deadlock if it improves parallelism
- · Deadlock avoidance may lead to livelock
 - may allow livelock if rare

Inserting Atomics

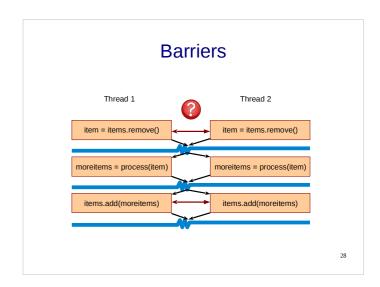
• Classwork: convert the following example from locks to atomics

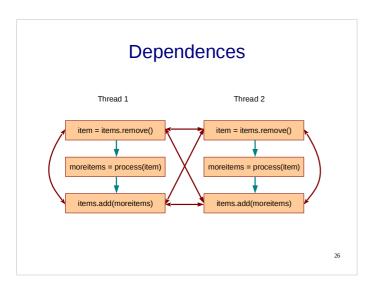
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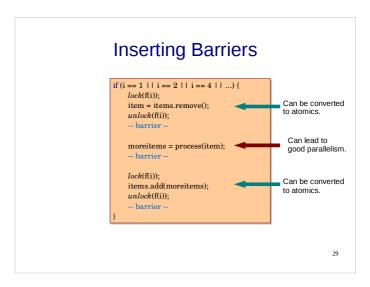
- Classwork: write parallel slist insertion and deletion routines using atomics
- **Homework:** write parallel dlist insertion routine using atomics

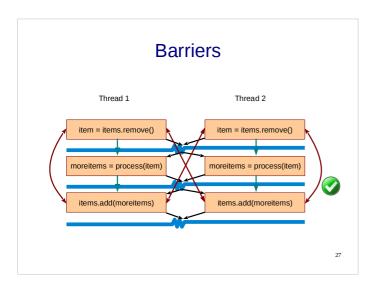
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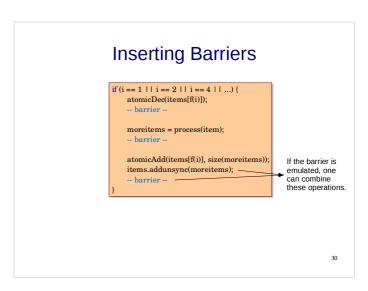
Inserting Locks if (i == 1 || i == 2 || i == 4 || ...) { lock(f(i)); item = items.remove(); moreitems = process(item); items.add(moreitems); unlock(f(i)); } If there are many threads involved in the if(...) condition and the operation is multi-step, overapproximate the dependences.







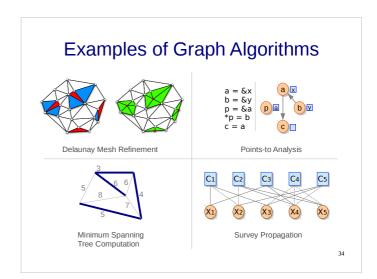


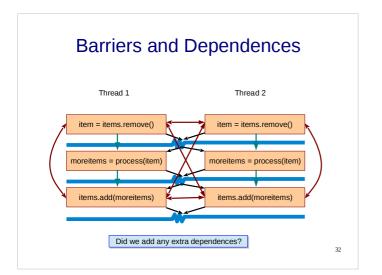


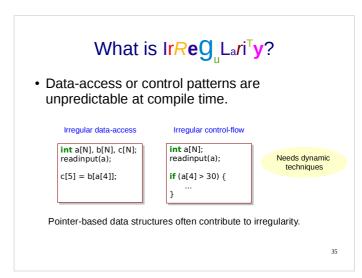
Barriers and Dependences

- A barrier may be considered in effect similar to loop distribution.
- If dependences are sparse, use atomics/locks; otherwise barriers work well.
- A barrier may add more dependences than required.
- But it must preserve all the existing dependences.

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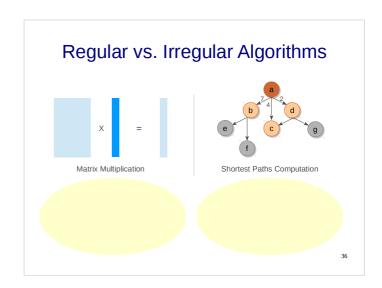


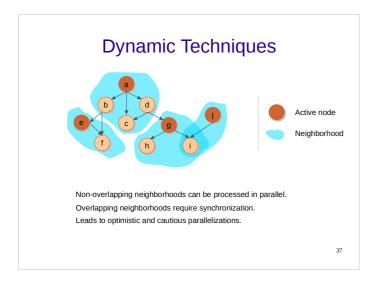




Limitations of Static Parallelization

- Some programs cannot be effectively parallelized using static techniques.
 - e.g. graph algorithms, pointer-savvy programs
- Existing static optimization techniques (analysis) are also very conservative for such programs.
- Ineffectiveness of static techniques forces us to use dynamic approaches.





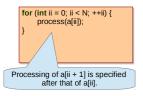
Sequential to Parallel

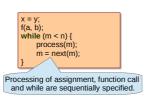
- · We added unorderedness.
- · We added non-determinism.
- We added higher-level information.

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Sequential to Parallel

• Sequential programs often overspecify dependencies.





We need a way to specify that various operations need not be executed in a specific order.

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for (int ii = 0; ii < N; ++ii) { process(a[ii]); } forall (e in a) { process(e); } unordered(x = y; f(a, b); while (m < n) { process(m); m = next(m); } unordered(x = y; f(a, b); while (m < n) { process(m); m = next(m); } };</pre>