

# Artificial Intelligence (CS6380)

**Constraint satisfaction**

# Search techniques considered till now

- **BFS, DFS, Uniform cost, Greedy Best First, A\*, IDA\***

- Systematic search methods
- All are complete on finite spaces
- Some have guarantees of optimality

- **Local search**

- Not systematic and hence incomplete
- Memory efficient, useful in infinite state spaces

Till now we assumed that state is atomic.

Can we have more details about the state? Use a factored representation

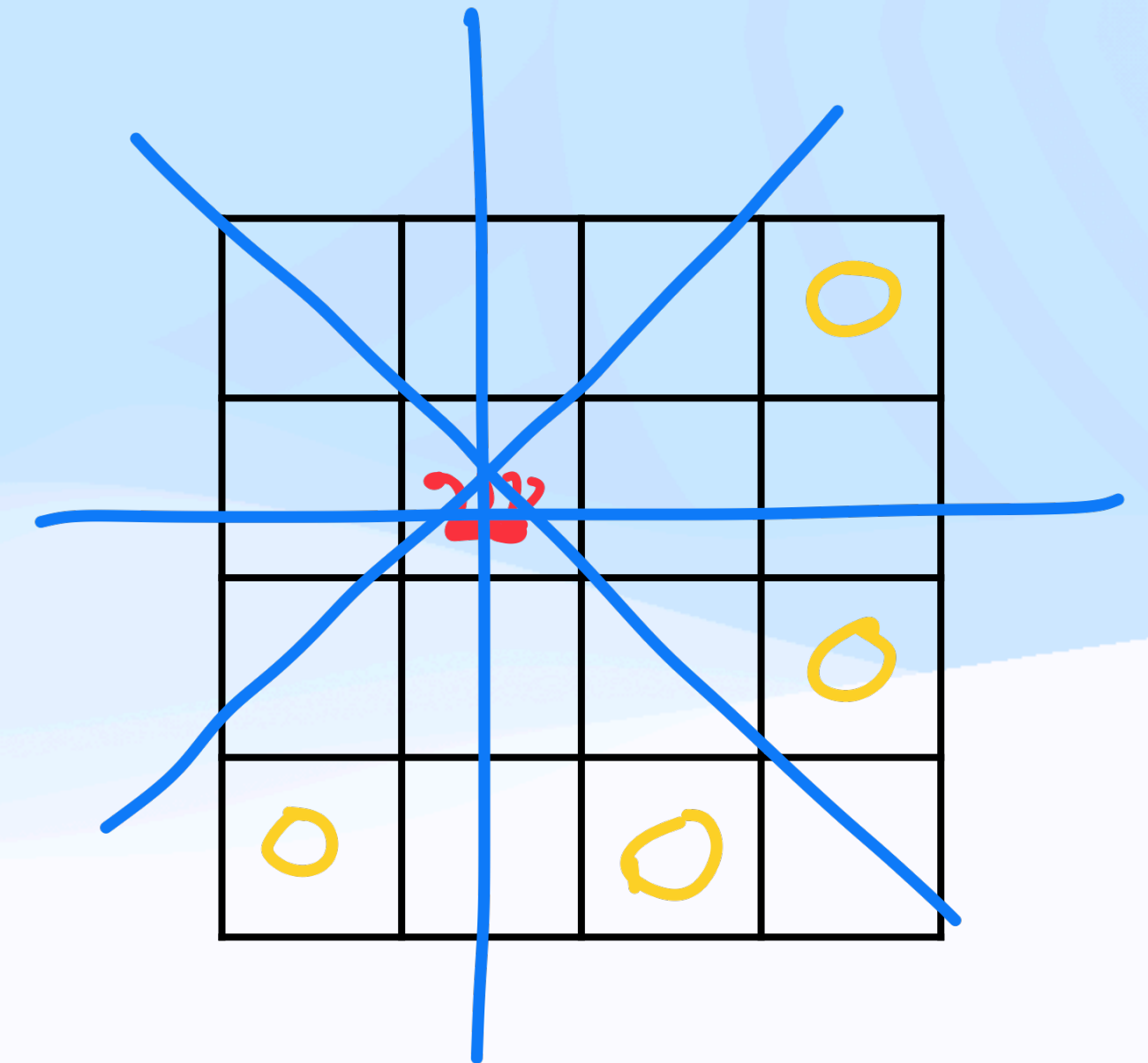
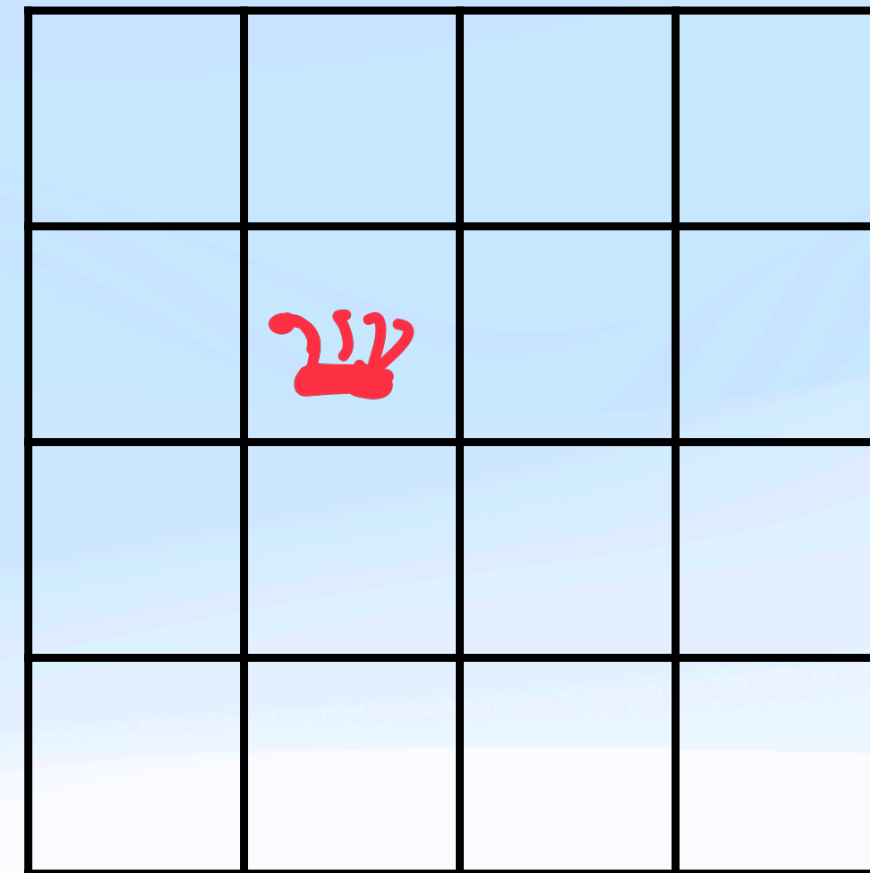
# N Queens problem

## N x N empty chess board

- Place N queens such that no queen is under attack by any other queen

## Possible approach:

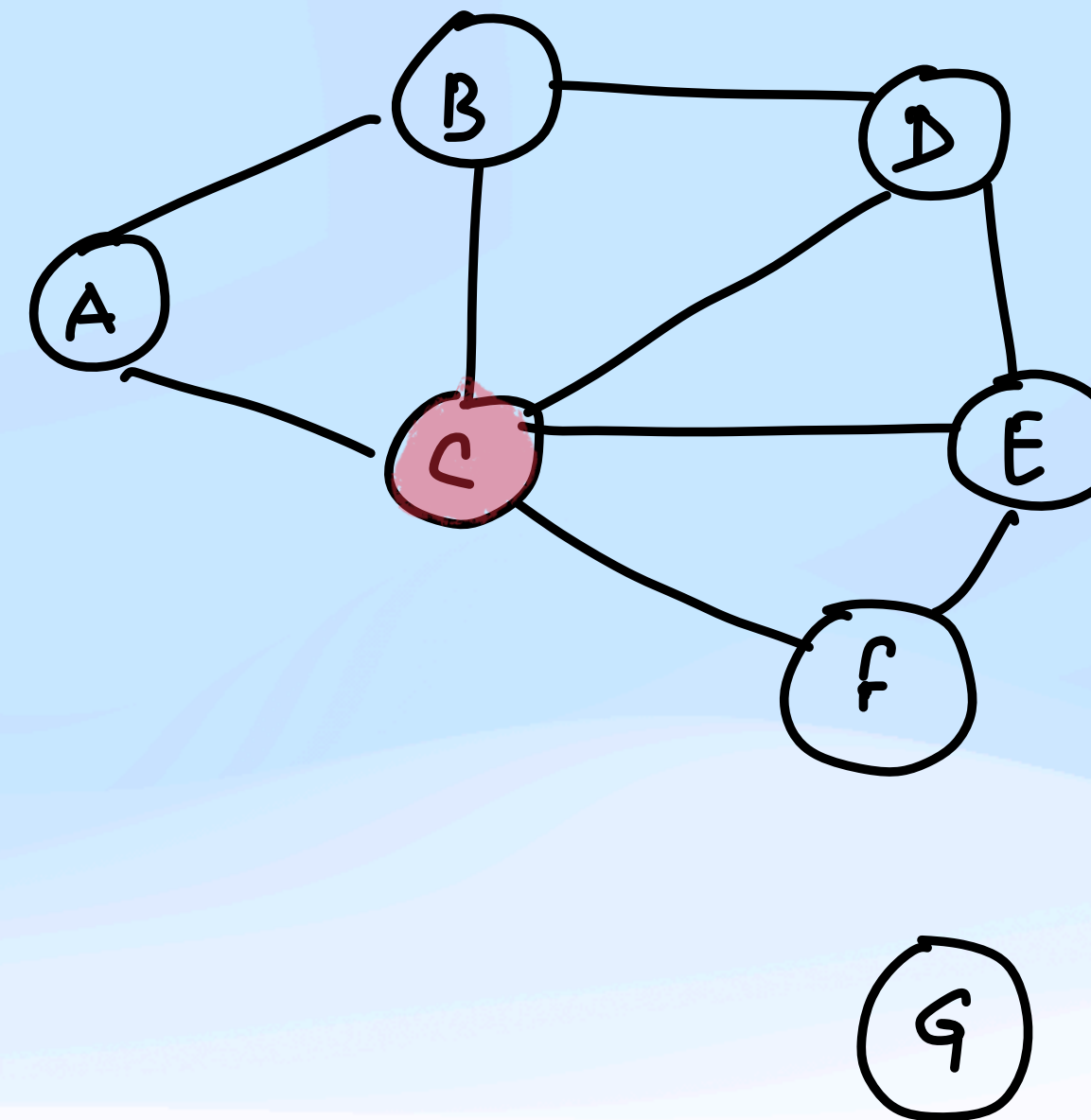
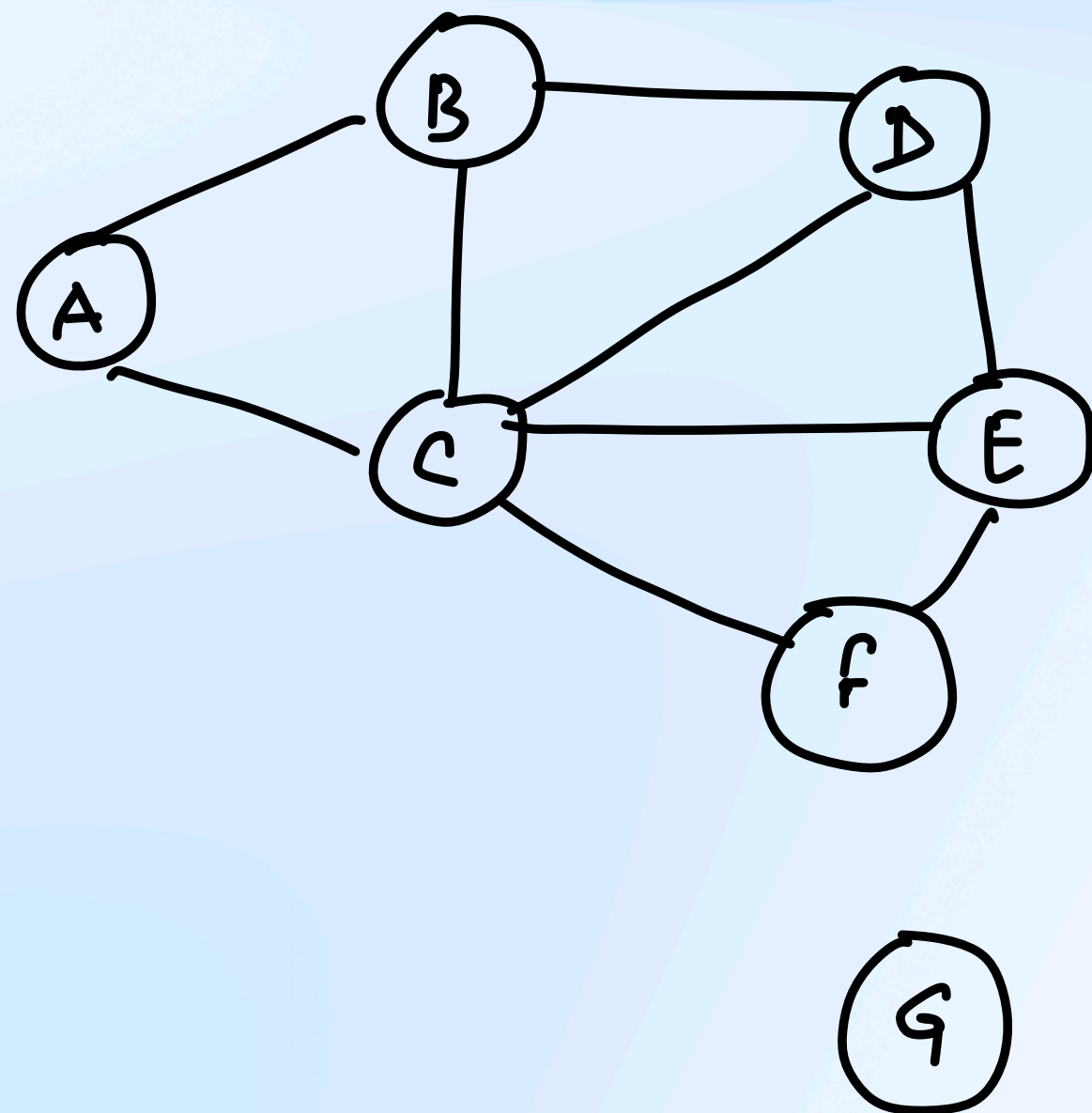
- Start one queen at a time, place the next queen
- If some queen is not placed, try placing it
- Check goal state



# Map colouring problem

## A map of a country

- Assign colours to regions so that adjacent regions are having different colours
- Equivalently vertex colouring of a graph





# Factored representation and CSP

## State

- Set of variables each of which has a value
- Variables have constraints

## Goal

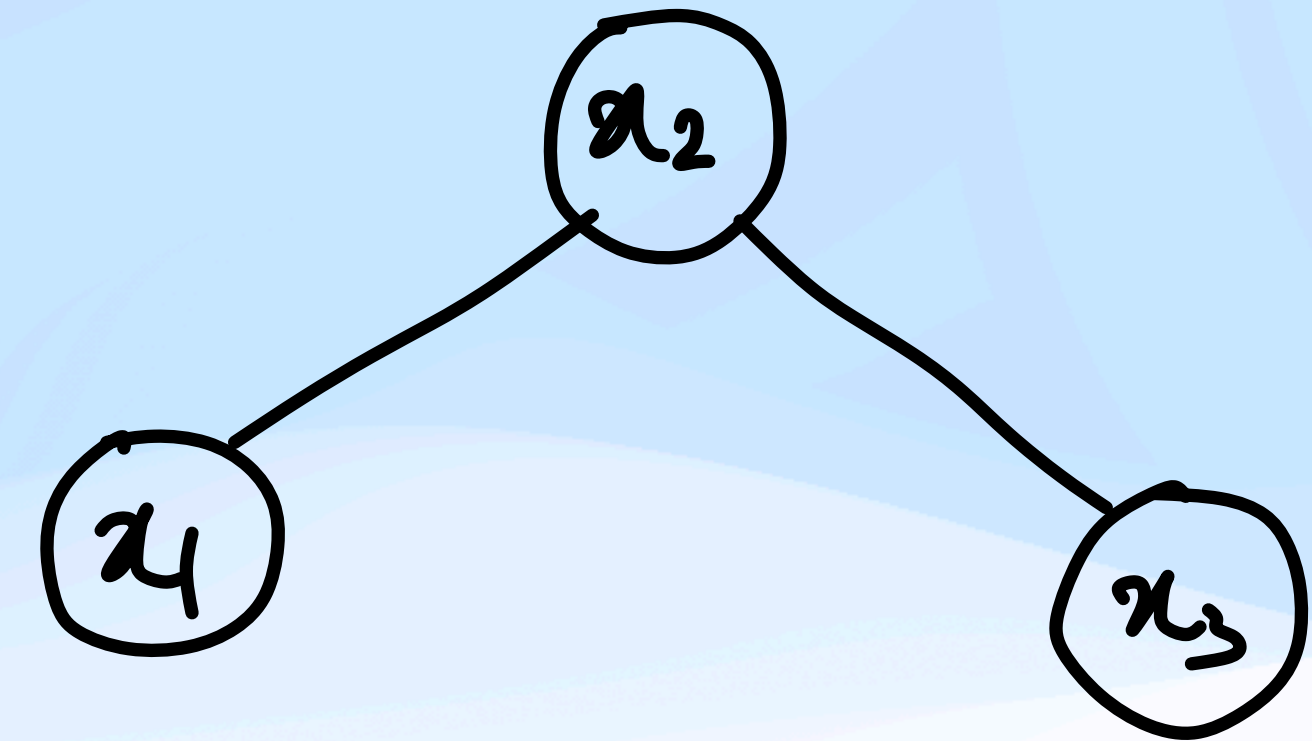
- Assignment of values to all variables such that constraints are satisfied

## Constraint satisfaction problem

- A set of variables  $\{ x_1, x_2, \dots, x_n \}$
- A set of domains  $\{ D_1, D_2, \dots, D_n \}$
- A set of constraints that specify allowable combinations of values

# CSP : first example

- $\{x_1, x_2, x_3\}$
- $D_1 = D_2 = D_3 = \{1, 2, 3\}$
- $C_{12}, C_{23}$

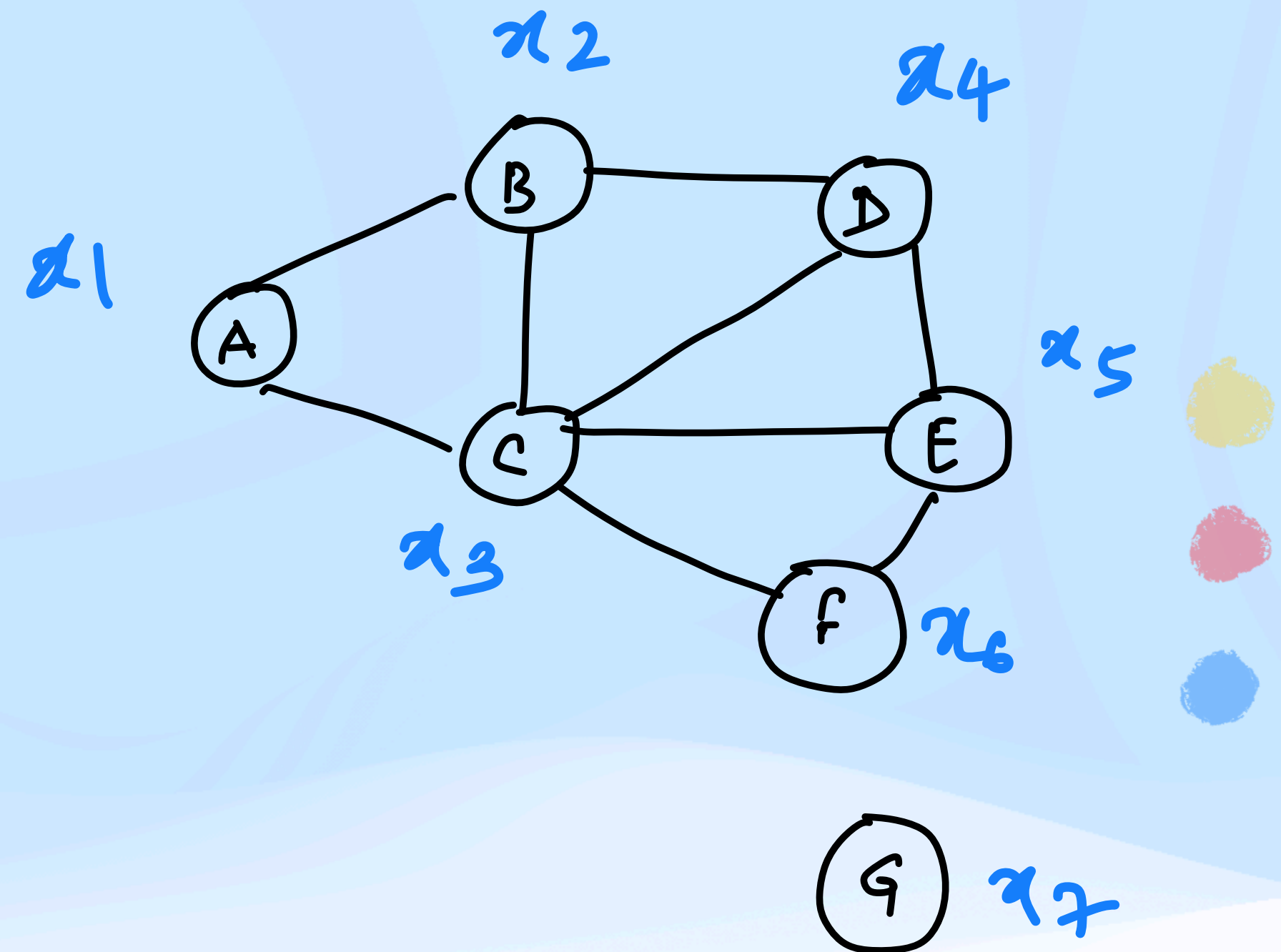
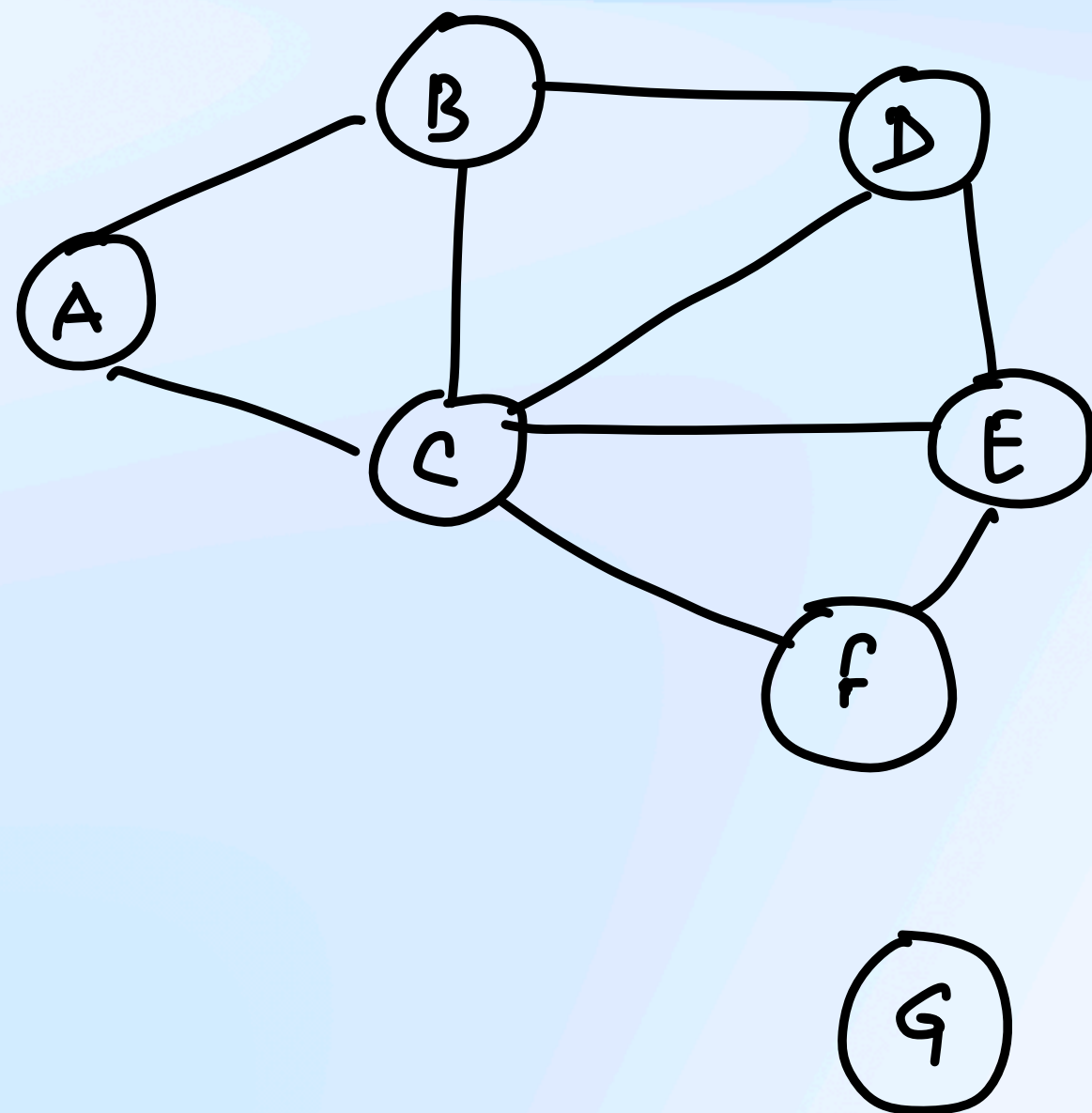


- **C12** :  $\{ \langle a, b \rangle \mid a \text{ in } D_1, b \text{ in } D_2, a < b \}$
- **C23** :  $\{ \langle a, b \rangle \mid a \text{ in } D_2, b \text{ in } D_3, a < b \}$
  
- **C12** :  $\{ \langle 1, 2 \rangle \langle 1, 3 \rangle \langle 2, 3 \rangle \}$
- **C23** :  $\{ \langle 1, 2 \rangle \langle 1, 3 \rangle \langle 2, 3 \rangle \}$

# Map colouring as CSP

## A map of a country

- Assign colours to regions so that adjacent regions are having different colours
- Equivalently vertex colouring of a graph

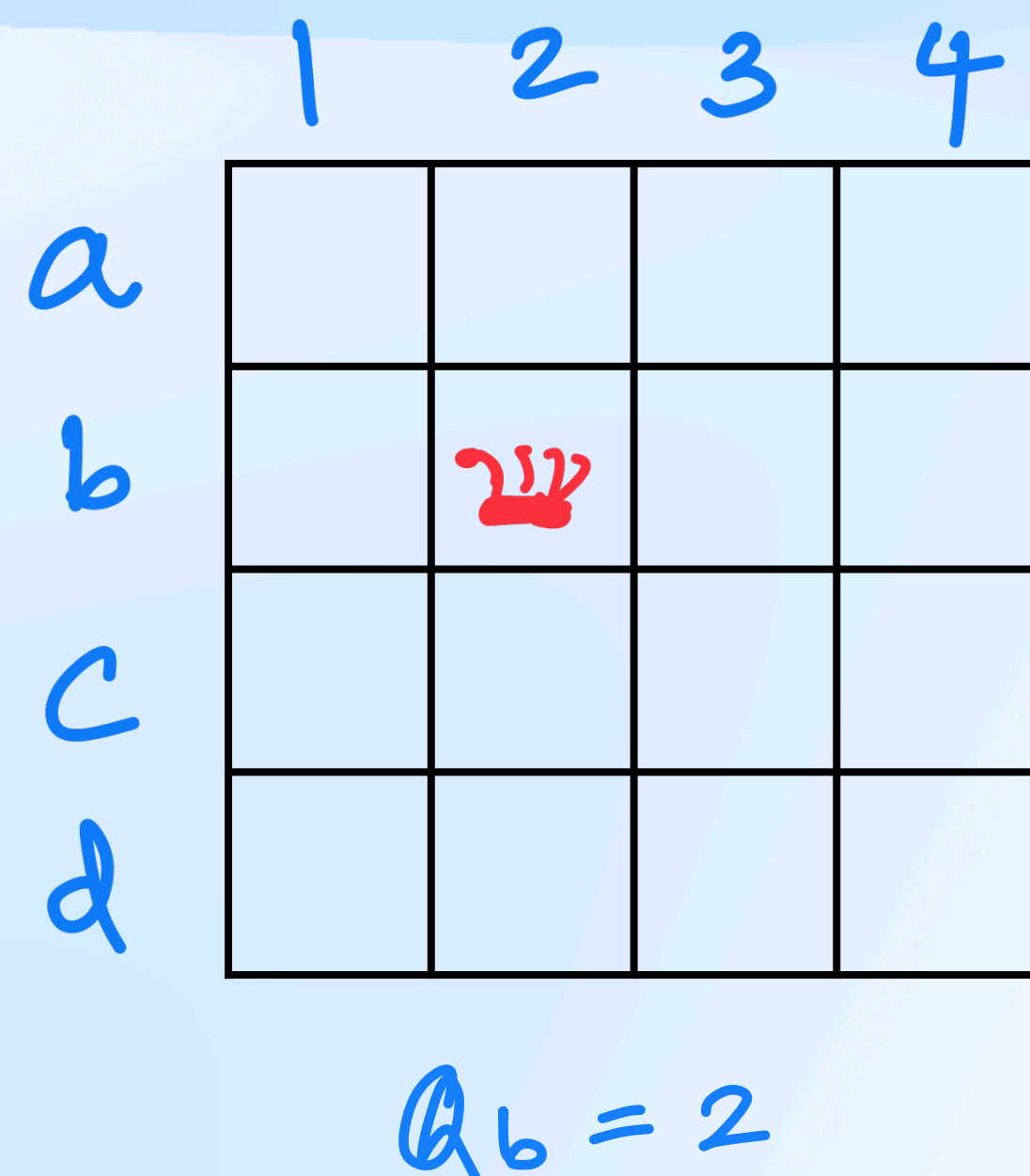


- **C12** : {  $\langle a, b \rangle \mid a \text{ in } D1, b \text{ in } D2, a \neq b$  }
- **C23** : {  $\langle a, b \rangle \mid a \text{ in } D2, b \text{ in } D3, a \neq b$  }
- ...

# N Queens as CSP

## N x N empty chess board

- Place N queens such that no queen is under attack by any other queen



Variables :  $Q_a$   $Q_b$   $Q_c$   $Q_d$

$Q_a$  is for row a

$Q_b$  is for row b

⋮

- C12** :  $\{ \langle x, y \rangle \mid x \text{ in } D1, y \text{ in } D2, x \neq y \}$
- C13** :  $\{ \langle x, y \rangle \mid x \text{ in } D2, y \text{ in } D3, x \neq y \}$
- ...

if  $Q_b = 2$  Can  $Q_c = 3$  ?  
 $Q_c = 1$  ?