Constraint	Iteration 0	Iteration 1	Iteration 2	Iteration 3
p = &a				
a = &x				
b = &y				
c = &z				
d = &w				
q = p				
a = b				
e = a				
r = q				
a = c				
s = r				
e = *a				
t = s				
a = d				
*e = a				

Constraint	Iteration 0	Iteration 1	Iteration 2	Iteration 3
p = &a	p → {a}			
a = &x	$a \rightarrow \{x\}$			
b = &y	$b \rightarrow \{y\}$			
c = &z	$C \rightarrow \{Z\}$			
d = &w	$d \rightarrow \{w\}$			
q = p				
a = b				
e = a				
r = q				
a = c				
s = r				
e = *a				
t = s				
a = d				
*e = a				

Constraint	Iteration 0	Iteration 1	Iteration 2	Iteration 3
p = &a	p → {a}			
a = &x	$a \rightarrow \{x\}$			
b = &y	$b \rightarrow \{y\}$			
c = &z	$C \rightarrow \{Z\}$			
d = &w	$d \rightarrow \{w\}$			
q = p				
a = b				
e = a				
r = q				
a = c				
s = r				
e = *a				
t = s				
a = d				
*e = a				

Constraint	Iteration 0	Iteration 1	Iteration 2	Iteration 3
p = &a	p → {a}			
a = &x	$a \rightarrow \{x\}$			
b = &y	$b \rightarrow \{y\}$			
c = &z	$C \rightarrow \{Z\}$			
d = &w	$d \rightarrow \{w\}$			
q = p		<b>q</b> → <b>{a}</b>		
a = b				
e = a				
r = q				
a = c				
s = r				
e = *a				
t = s				
a = d				
*e = a				

Constraint	Iteration 0	Iteration 1	Iteration 2	Iteration 3
p = &a	p → {a}			
a = &x	$a \rightarrow \{x\}$			
b = &y	$b \rightarrow \{y\}$			
c = &z	$C \rightarrow \{Z\}$			
d = &w	$d \rightarrow \{w\}$			
q = p		$q \rightarrow \{a\}$		
a = b		a → {y}		
e = a		e → {x,y}		
r = q				
a = c				
s = r				
e = *a				
t = s				
a = d				
*e = a				

Constraint	Iteration 0	Iteration 1	Iteration 2	Iteration 3
p = &a	p → {a}			
a = &x	$a \rightarrow \{x\}$			
b = &y	$b \rightarrow \{y\}$			
c = &z	$C \rightarrow \{Z\}$			
d = &w	$d \rightarrow \{M\}$			
q = p		$q \rightarrow \{a\}$		
a = b		$a \rightarrow \{y\}$		
e = a		$e \rightarrow \{x,y\}$		
r = q		$r \rightarrow \{a\}$		
a = c		a → {z}		
s = r		$s \rightarrow \{a\}$		
e = *a				
t = s				
a = d				
*e = a				

Constraint	Iteration 0	Iteration 1	Iteration 2	Iteration 3
p = &a	p → {a}			
a = &x	$a \rightarrow \{x\}$			
b = &y	$b \rightarrow \{y\}$			
c = &z	$C \rightarrow \{Z\}$			
d = &w	$d \rightarrow \{m\}$			
q = p		$q \rightarrow \{a\}$		
a = b		$a \rightarrow \{y\}$		
e = a		$e \rightarrow \{x,y\}$		
r = q		$r \rightarrow \{a\}$		
a = c		$a \rightarrow \{z\}$		
s = r		$s \rightarrow \{a\}$		
e = *a				
t = s				
a = d				
*e = a				

Constraint	Iteration 0	Iteration 1	Iteration 2	Iteration 3
p = &a	p → {a}			
a = &x	$a \rightarrow \{x\}$			
b = &y	$b \rightarrow \{y\}$			
c = &z	$C \rightarrow \{Z\}$			
d = &w	$d \rightarrow \{w\}$			
q = p		$q \rightarrow \{a\}$		
a = b		$a \rightarrow \{y\}$		
e = a		$e \rightarrow \{x,y\}$		
r = q		$r \rightarrow \{a\}$		
a = c		a → {z}		
s = r		$s \rightarrow \{a\}$		
e = *a				
t = s		$t \rightarrow \{a\}$		
a = d		$a \rightarrow \{w\}$		
*e = a				

Constraint	Iteration 0	Iteration 1	Iteration 2	Iteration 3
p = &a	p → {a}			
a = &x	$a \rightarrow \{x\}$			
b = &y	$b \rightarrow \{y\}$			
c = &z	$C \rightarrow \{z\}$			
d = &w	$d \rightarrow \{w\}$			
q = p		$q \rightarrow \{a\}$		
a = b		$a \rightarrow \{y\}$		
e = a		$e \rightarrow \{x,y\}$		
r = q		$r \rightarrow \{a\}$		
a = c		$a \rightarrow \{z\}$		
s = r		$s \rightarrow \{a\}$		
e = *a				
t = s		t → {a}		
a = d		$a \rightarrow \{w\}$		
<b>4</b>				

Constraint	Iteration 0	Iteration 1	Iteration 2	Iteration 3
p = &a	p → {a}			
a = &x	a → {x}			
b = &y	$b \rightarrow \{y\}$			
c = &z	$C \rightarrow \{Z\}$			
d = &w	$d \rightarrow \{w\}$			
q = p		$q \rightarrow \{a\}$		
a = b		a → {y}		
e = a		e → {x,y}		
r = q		$r \rightarrow \{a\}$		
a = c		a → {z}		
s = r		$s \rightarrow \{a\}$		
e = *a				
t = s		$t \rightarrow \{a\}$		
a = d		a → {w}		
*e = a		$x,y \rightarrow \{x,y,z,w\}$		

Constraint	Iteration 0	Iteration 1	Iteration 2	Iteration 3
p = &a	p → {a}			
a = &x	$a \rightarrow \{x\}$			
b = &y	$b \rightarrow \{y\}$			
c = &z	$C \rightarrow \{Z\}$			
d = &w	$d \rightarrow \{w\}$			
q = p		$q \rightarrow \{a\}$		
a = b		$a \rightarrow \{y\}$		
e = a		$e \rightarrow \{x,y\}$	$e \rightarrow \{z,w\}$	
r = q		$r \rightarrow \{a\}$		
a = c		$a \rightarrow \{z\}$		
s = r		$s \rightarrow \{a\}$		
e = *a				
t = s		$t \rightarrow \{a\}$		
a = d		a → {w}		
*e = a		$x,y \rightarrow \{x,y,z,w\}$	$Z,W \rightarrow \{X,y,Z,W\}$	

Constraint	Iteration 0	Iteration 1	Iteration 2	Iteration 3
p = &a	p → {a}			
a = &x	$a \rightarrow \{x\}$			
b = &y	$b \rightarrow \{y\}$			
c = &z	$C \rightarrow \{z\}$			
d = &w	$d \rightarrow \{w\}$			
q = p		$q \rightarrow \{a\}$		
a = b		$a \rightarrow \{y\}$		int
e = a		$e \rightarrow \{x,y\}$	$e \rightarrow \{z,w\}$	fixed-point
r = q		$r \rightarrow \{a\}$		ixec
a = c		$a \rightarrow \{z\}$		
s = r		$s \rightarrow \{a\}$		
e = *a				
t = s		$t \rightarrow \{a\}$		
a = d		a → {w}		
*e = a		$x,y \rightarrow \{x,y,z,w\}$	$z,w \rightarrow \{x,y,z,w\}$	

Constraint	Iteration 0	Iteration 1	lieration 2	Iteration 3
p = &a	p → {a}			
a = &x	$a \rightarrow \{x\}$			
b = &y	$b \rightarrow \{y\}$		13 ste	eps
c = &z	$C \rightarrow \{Z\}$			
d = &w	$d \rightarrow \{w\}$			
q = p		$q \rightarrow \{a\}$		
a = b		$a \rightarrow \{y\}$		int
e = a		$e \rightarrow \{x,y\}$	$e \rightarrow \{z,w\}$	fixed-point
r = q		$r \rightarrow \{a\}$		ixec
a = c		$a \rightarrow \{z\}$		
s = r		$s \rightarrow \{a\}$		
e = *a				
t = s		t → {a}		
a = d		a → {w}		
*e = a		$x,y \rightarrow \{x,y,z,w\}$	$z,w \rightarrow \{x,y,z,w\}$	

#### Outline

Introduction

Basics! What people already know.

Parallel Points-to Analysis

Cryptic! What people fail to know.

- Naïve method
- Replication-based approach
- Optimizations

Details! What people need not know.

Results

Horror! What people should not know.

Constraint	Iteration 0	Iteration 1	Iteration 2	Iteration 3
p = &a				
a = &x				
b = &y				
c = &z				
d = &w				
q = p				
a = b				
e = a				
r = q				
a = c				
s = r				
e = *a				
t = s				
a = d				
*e = a				

Constraint	Iteration 0	Iteration 1	Iteration 2	Iteration 3
p = &a				
a = &x				
b = &y				
c = &z				
d = &w				
q = p				
a = b				
e = a				
r = q				
<b>a</b> = <b>c</b>				
s = r				
e = *a				
t = s				
<b>a</b> = <b>d</b>				
*e = a				

Constraint	Iteration 0	Iteration 1	Iteration 2	Iteration 3
p = &a				
a = &x				
b = &y				
c = &z				
d = &w				
q = p				
a = b				
e = a				
r = q				
a = c				
s = r				
e = *a				
t = s				
a = d				
*e = a				

### **Conflicting Constraints**

Two constraints conflict if at least one of them writes to a common variable.

Points-to constraints	Read-Set	Write-Set	
<pre>p = &amp;q address-of p = q copy p = *q load *p = q store</pre>	{ } {q} {q} U {x: q → {x}} {q, p}	{p} {p} {p} {x: p → {x}}	

Constraint	Iteration 0	Iteration 1	Iteration 2	Iteration 3
p = &a				
a = &x				
b = &y				
c = &z				
d = &w				
q = p				
a = b				
e = a				
r = q				
a = c				
s = r				
e = *a				
t = s				
<b>a</b> = <b>d</b>				
*e = a				

Thread1	Thread2
<b>a</b> = <b>b</b>	q = p
$\mathbf{a} = \mathbf{c}$	r = q
<b>a</b> = <b>d</b>	s = r
e = *a	t = s
<b>e</b> = <b>a</b>	
*e = a	

9 steps

Thread1	Thread2
a = b	q = p
<b>a</b> = <b>c</b>	r = q
a = d	s = r
e = *a	t = s
e = a	
*e = a	

Sequential: 13 steps.

Even if the analysis is provided with 8 cores, the parallel analysis still requires 9 steps.

- 1. Find conflicting constraints.
- 2. Schedule constraints.
- 3. Analyze in parallel.
- 4. Update points-to information.

- 1. Find conflicting constraints.
- 2. Schedule constraints.
- 3. Analyze in parallel.
- . Update points-to information.

Find conflicting constraints.
 Schedule constraints.
 Analyze in parallel.
 Update points-to information.

- 1. Find conflicting constraints.
- 2. Schedule constraints.
- 3. Analyze in parallel.
- . Update points-to information.

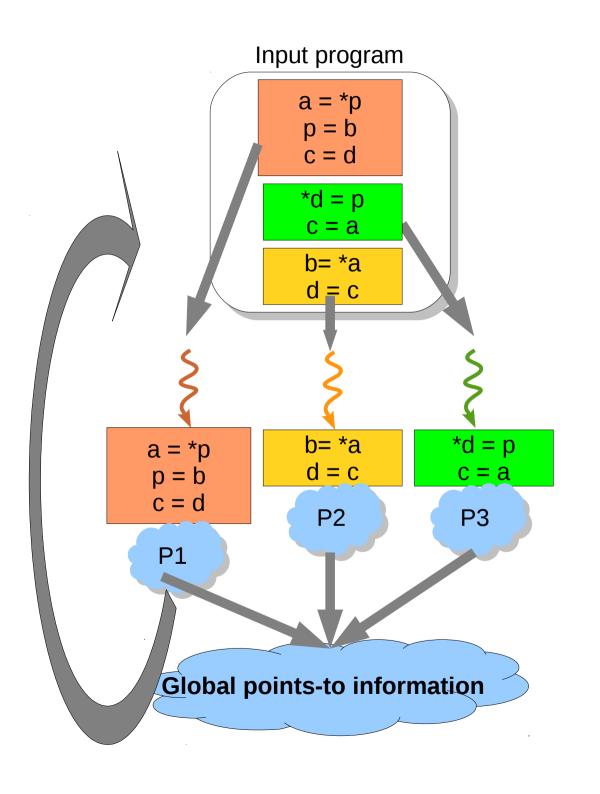
- 1. Find conflicting constraints.
- 2. Schedule constraints.
- 3. Analyze in parallel.
- . Update points-to information.

- 1. Find conflicting constraints.
- 2. Schedule constraints.

3. Analyze in parallel. Straightforward

**Simple** 

- 1. Find conflicting constraints.
- 2. Schedule constraints.
- 3. Analyze in parallel.
  - Initial reads from the master copy.
  - · Writes to local replica.
- 4. Update points-to information.
  - Merge local replicas with the master copy.



Arbitrary
Partition
(points-to constraints)

Parallel Execution (replicated points-to)

Merge (global points-to)

### Why Replication Works

- 1. Monotonically increasing computation.
  - Points-to sets never shrink.
- 2. Unordered algorithm.
  - · Constraints can be processed in any order.

For instance, a naïve replication doesn't work for flow-sensitive analysis.

Constraint	Iteration 0	Iteration 1	Iteration 2	Iteration 3
p = &a				
a = &x				
b = &y				
c = &z				
d = &w				
q = p				
a = b				
e = a				
r = q				
a = c				
s = r				
e = *a				
t = s				
a = d				
*e = a				

Constraint	Iteration 0	Iteration 1	Iteration 2	Iteration 3
q = p				
a = b				
e = a				
r = q				
a = c				
s = r				
e = *a				
t = s				
a = d				
*e = a				

Т	Stmt	Itr 1	Merge 1	Itr 2	Merge 2	Itr 3	Merge 3
1	q = p						
	a = b						
	e = a						
	r = q						
2	a = c						
	s = r						
	e = *a						
3	t = s						
	a = d						
	*e = a						

Т	Stmt	Itr 1	Merge 1	Itr 2	Merge 2	Itr 3	Merge 3
1	q = p	q' → {a}					
	a = b	a' → {y}					
	e = a	$e' \rightarrow \{x, y\}$					
	r = q	r' → {a}					
2	a = c	a'' → {z}					
	s = r						
	e = *a						
3	t = s						
	a = d	a''' → {w}					
	*e = a						

Т	Stmt	Itr 1	Merge 1	Itr 2	Merge 2	Itr 3	Merge 3
1	q = p	q' → {a}					
	a = b	a' → {y}					
	e = a	$e' \rightarrow \{x, y\}$					
	r = q	r' → {a}	$a \rightarrow \{y, z, w\}$				
2	a = c	a'' → {z}	$e \rightarrow \{x, y\}$				
	s = r		$q, r \rightarrow \{a\}$				
	e = *a						
3	t = s						
	a = d	a''' → {w}					
	*e = a						

Т	Stmt	Itr 1	Merge 1	Itr 2	Merge 2	Itr 3	Merge 3
1	q = p	q' → {a}					
	a = b	a' → {y}					
	e = a	$e' \rightarrow \{x, y\}$		$e' \rightarrow \{x,y,z,w\}$			
	r = q	r' → {a}	$a \rightarrow \{y, z, w\}$		$e \rightarrow \{y,z,w\}$		$z,w \rightarrow \{x,y,z,w\}$
2	a = c	$a'' \rightarrow \{z\}$	$e \rightarrow \{x, y\}$		$X \rightarrow \{X, y, Z, W\}$		t → {a}
	s = r		$q, r \rightarrow \{a\}$	s' → {a}	$s \rightarrow \{a\}$		
	e = *a						
3	t = s					t' → {a}	
	a = d	a''' → {w}					
	*e = a			$X', y' \rightarrow \{X, y, Z, W\}$		$Z',W' \rightarrow \{X,Y,Z,W\}$	

Т	Stmt	Itr 1	Merge 1	Itr 2	Merge 2	Itr 3	Merge 3
1	q = p	$q' \rightarrow \{a\}$					
	a = b	$a' \rightarrow \{y\}$				12 ste	ps
	e = a	$e' \rightarrow \{x, y\}$		$e' \rightarrow \{x,y,z,w\}$			
	r = q	r' → {a}	$a \rightarrow \{y, z, w\}$		$e \rightarrow \{y,z,w\}$		$z,w \rightarrow \{x,y,z,w\}$
2	a = c	$a'' \rightarrow \{z\}$	$e \rightarrow \{x, y\}$		$X \rightarrow \{x,y,z,w\}$		t → {a}
	s = r		$q, r \rightarrow \{a\}$	s' → {a}	$s \rightarrow \{a\}$		
	e = *a						
3	t = s					t' → {a}	
	a = d	a''' → {w}					
	*e = a			$X', y' \rightarrow \{X, y, Z, W\}$		$Z',W' \rightarrow \{X,y,Z,W\}$	

Sequential: 13 steps, Parallel: 9 steps.

### Naïve vs. Replication-based

Pros	Cons
No merging	Costly merging
Lesser iterations	More iterations
General purpose	Monotonic, unordered
Lower memory requirement	Higher memory requirement

Cons	Pros
Costly conflict-detection	No conflict-detection
Limited parallelism	Adaptive parallelism
Unbalanced load	Better load-balancing
Lower parallel performance	Better parallel performance

Т	Stmt	Itr 1	Merge 1	Itr 2	Merge 2	Itr 3	Merge 3
1	q = p						
	e = a						
2	r = q						
	a = c						
3	e = *a						
	s = r						
	t = s						
	a = d						
4	*e = a						
	a = b						

Т	Stmt	Itr 1	Merge 1	Itr 2	Merge 2	Itr 3	Merge 3
1	q = p	q' → {a}					
	e = a	$e' \rightarrow \{x\}$		$e' \rightarrow \{y,z,w\}$			
2	r = q			$r' \rightarrow \{a\}$			
	a = c	a'' → {z}	$a \rightarrow \{y, z, w\}$		$e \rightarrow \{y,z,w\}$		$y,z,w \rightarrow \{x,y,z,w\}$
3	e = *a		$e \rightarrow \{x\}$		$X \rightarrow \{x,y,z,w\}$		$s,t \rightarrow \{a\}$
	s = r		$q \rightarrow \{a\}$		$r \rightarrow \{a\}$		
	t = s					$s',t' \rightarrow \{a\}$	
	a = d	a''' → {w}					
4	*e = a			$X' \rightarrow \{X,y,Z,W\}$		$y',Z',W' \rightarrow \{x,y,z,W\}$	
	a = b	a' → {y}					

Т	Stmt	Itr 1	Merge 1	Itr 2	Merge 2	Itr 3	Merge 3
1	q = p	$q' \rightarrow \{a\}$					
	e = a	$e' \rightarrow \{x\}$		$e' \rightarrow \{y,z,w\}$		9 step	os
2	r = q			r' → {a}			
	a = c	a'' → {z}	$a \rightarrow \{y, z, w\}$		$e \rightarrow \{y,z,w\}$		y,z,w → {x,y,z,w}
3	e = *a		$e \rightarrow \{x\}$		$X \rightarrow \{X,y,Z,W\}$		$s,t \rightarrow \{a\}$
	s = r		$q \rightarrow \{a\}$		$r \rightarrow \{a\}$		
	t = s					s',t' → {a}	
	a = d	a''' → {w}					
4	*e = a			$X' \rightarrow \{X,y,Z,W\}$		$y',Z',W' \rightarrow \{X,y,Z,W\}$	
	a = b	a' → {y}					

Sequential: 13 steps, Parallel: 9 steps. Replication with 3 threads: 12 steps.

Т	Stmt	Itr 1	Merge 1	Itr 2	Merge 2	Itr 3	Merge 3
1	e = a	$e' \rightarrow \{x\}$		$e' \rightarrow \{y,z,w\}$			
2	q = p	$q' \rightarrow \{a\}$					
3	r = q			r' → {a}			
	a = c	a'' → {z}	$a \rightarrow \{y, z, w\}$		$e \rightarrow \{y,z,w\}$		$y,z,w \rightarrow \{x,y,z,w\}$
4	e = *a		$e \rightarrow \{x\}$		$X \rightarrow \{X,y,Z,W\}$		$s,t \rightarrow \{a\}$
	s = r		$q \rightarrow \{a\}$		$r \rightarrow \{a\}$		
	t = s					s',t' → {a}	
	a = d	$a''' \rightarrow \{w\}$					
5	*e = a			$X' \rightarrow \{X,y,Z,W\}$		$y',Z',W' \rightarrow \{x,y,z,W\}$	
	a = b	$a' \rightarrow \{y\}$					

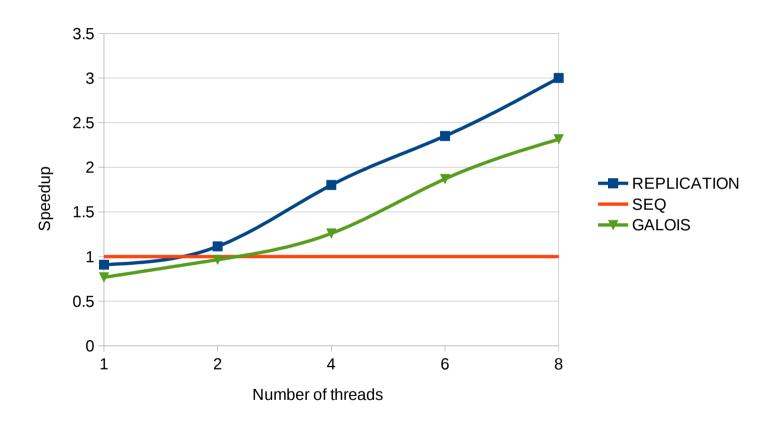
Т	Stmt	Itr 1	Merge 1	Itr 2	Merge 2	Itr 3	Merge 3
1	e = a	e' → {x}		$e' \rightarrow \{y,z,w\}$			
2	q = p	$q' \rightarrow \{a\}$				8 step	os
3	r = q			$r' \rightarrow \{a\}$			
	a = c	a'' → {z}	$a \rightarrow \{y, z, w\}$		$e \rightarrow \{y,z,w\}$		$y,z,W \rightarrow \{x,y,z,W\}$
4	e = *a		$e \rightarrow \{x\}$		$X \rightarrow \{X,y,Z,W\}$		$s,t \rightarrow \{a\}$
	s = r		$q \rightarrow \{a\}$		$r \rightarrow \{a\}$		
	t = s					s',t' → {a}	
	a = d	a''' → {w}					
5	*e = a			$X' \rightarrow \{X,y,Z,W\}$		$y',Z',W' \rightarrow \{x,y,z,W\}$	
	a = b	a' → {y}					

Sequential: 13 steps, Parallel: 9 steps. Replication with 3 threads: 12 steps. Replication with 4 threads: 9 steps.

### Optimizations

- Load Balancing
  - Orphan-and-Adopt approach.
  - store constraints are the culprits.
  - Trade-off between load-balancing and thread-communication.
- Parallel Online Cycle Elimination
  - Disjoint cycles can be collapsed in parallel.
- Reducing Replication Cost
  - Single writer.
  - Difference propagation.
  - Constraint affinity.
- Limited Scheduling

#### Results



Benchmarks: 16 SPEC 2K + 5 open-source