

Lists

Rupesh Nasre.
rupesh@iitm.ac.in

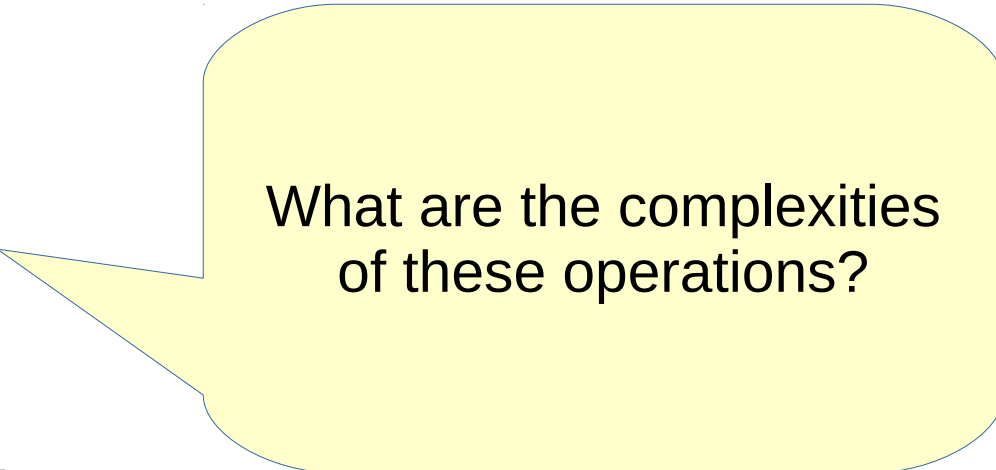
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ADT

- Abstract Data Type
- Defines the **interface** of the functionality provided by the data structure.
- Hides implementation details.
 - Defines *what* and hides *how*.
- Makes software modular.
- Allows easy change of implementation.

List as an ADT

```
class List {  
public:  
    List();  
    void insert(Element e);  
    void find(Element e);  
    void remove(Element e);  
    void print();  
    int size();  
};
```



What are the complexities of these operations?

Other ADTs

- Fan regulator
 - IncSpeed, decSpeed, getSpeed, getCompanyName
- Integer
 - size, isSigned, getValue, setValue, add, sub
- Student
 - getRollNo, getHostel, getFavGame, setHostel, getSlots, setCGPA

List using Array

```
class List {
```

```
public:
```

```
    List();
```

```
    void insert(Element e);
```

```
    void find(Element e);
```

```
    void remove(Element e);
```

```
    void print();
```

```
    int size();
```

```
};
```

4	2	7	2	9			
---	---	---	---	---	--	--	--

Design decisions

- Size of the array?
- Maintain size separately or use a sentinel?
- On overflow: error or realloc?
- On underflow: error message or exit or silent?
- Printing order?
- Duplicates allowed?
- For duplicates, what does remove do?
- ...

List using Array

```
class List {
```

```
public:
```

```
    List();
```

```
    void insert(Element e);    O(1)
```

```
    void find(Element e);     O(N)
```

```
    void remove(Element e); O(N)
```

```
    void print();             O(N)
```

```
    int size();               O(1)
```

```
};
```

4	2	7	2	9			
---	---	---	---	---	--	--	--

List using Linked List

```
class List {
```

```
public:
```

```
    List();
```

```
    void insert(Element e);    O(N) without tail pointer, else O(1)
```

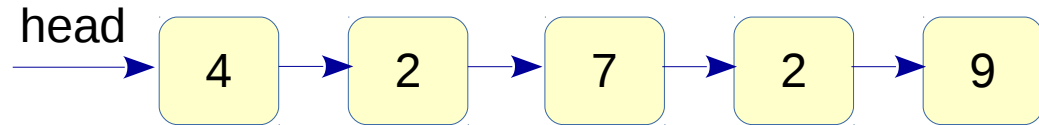
```
    void find(Element e);    O(N)
```

```
    void remove(Element e); O(N)
```

```
    void print();    O(N)
```

```
    int size();    O(1)
```

```
};
```



If the complexities of array-based versus linked-list-based implementations are the same, **why use linked lists?**

Arrays versus Linked Lists

- Need to copy the existing array on reallocation.
- Removal of i th element needs element shifting from $i+1$ to end.
- Same with insertion.
- Array concatenation is linear time.
- Only a link needs to be established ($O(1)$).
- Removal of an element using pointers can be done in $O(1)$.
- Same with insertion.
- List concatenation is $O(1)$.

Linked List Implementation

- Source: **sll.cpp**

Surprise Quiz

Declare the following:

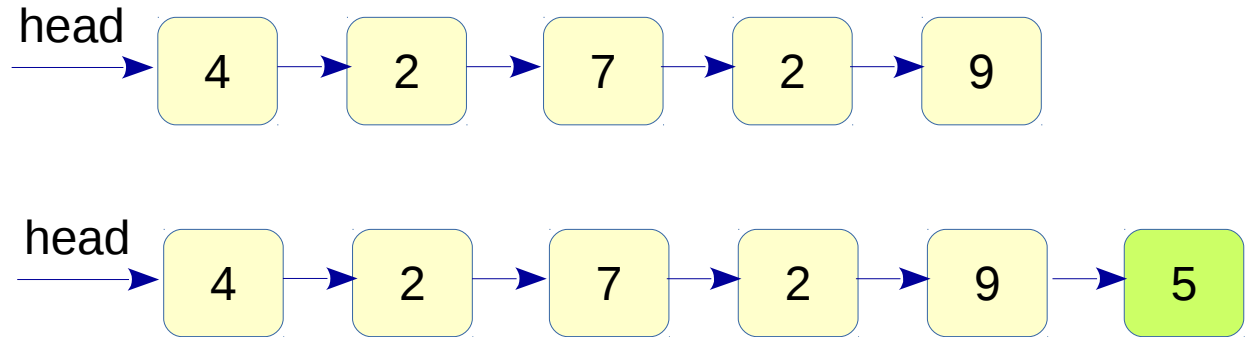
- Pointer to integer
- Pointer to pointer to integer
- Pointer to array of integers
- Array of pointers to integers
- Access the value in the second node of a linked list pointed to by head.

What does this do?

- `*((*ptr).next).val = x;`
- `x = *ptr++; y = (*ptr)++; z = *++ptr; w = ++*ptr;`

List insert

- insert(5)



Setup node:

```
Node *newptr = new Node();  
newptr->val = 5;  
newptr->next = NULL;
```

End case:

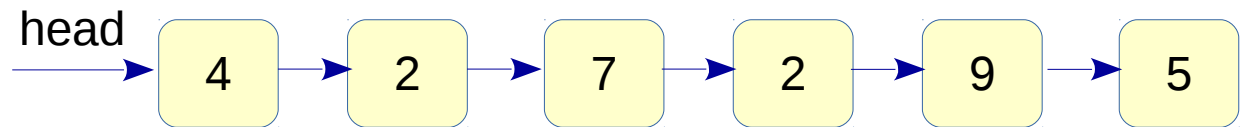
```
if (head == NULL) head = newptr;
```

Regular case:

```
for (Node *ptr = head; ptr->next; ptr = ptr->next)  
    ;  
ptr->next = newptr;
```

List print

- print()



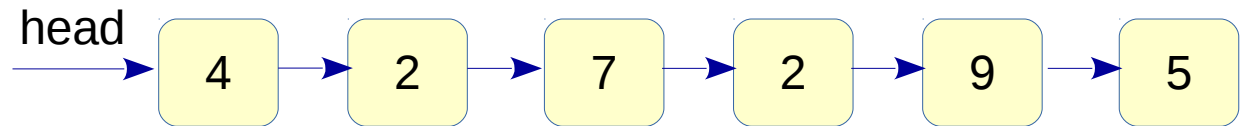
Output: 4 2 7 2 9 5

For each element in the list
Print the element

```
for (Node *ptr = head; ptr; ptr = ptr->next)
    printf("%c ", ptr->val);
printf("\n");
```

List find

- find(9)



For each element in the list

 If the element is same as that to be searched

 Found the element

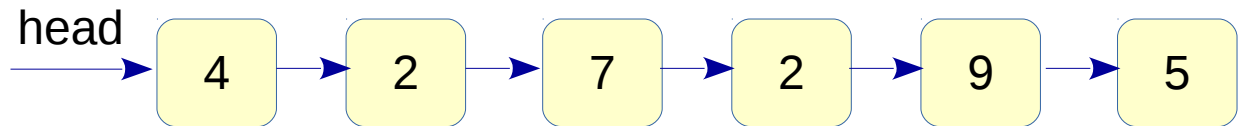
Element not present

```
for (Node *ptr = head; ptr; ptr = ptr->next)
    if (ptr->val == val) return true;
return false;
```

List remove

- remove(2)
- remove(5)
- remove(4)

On your demand,
we want to
remove all
occurrences of the
value.



Special case:

if (head == NULL) return false;

General case:

```
Node *previous = NULL;
for (Node *ptr = head; ptr;) {
    if (ptr->val == val) {
        Node *toberemoved = ptr;
        if (previous) {
            previous->next = ptr->next;
        } else head = ptr->next;
        ptr = ptr->next;
        free(toberemoved);
        removed = true;
    } else {
        previous = ptr;
        ptr = ptr->next;
    }
}
```

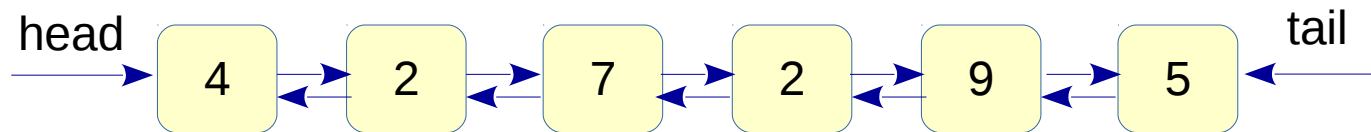
Pitfalls

- `ptr = head->next;` // segfault. Check if head is NULL.
- `Node *ptr = &node1; return;` // local variable node1.
- `Ptr = malloc(sizeof(Node*));` // insufficient memory.

Wrong **deleteList** program

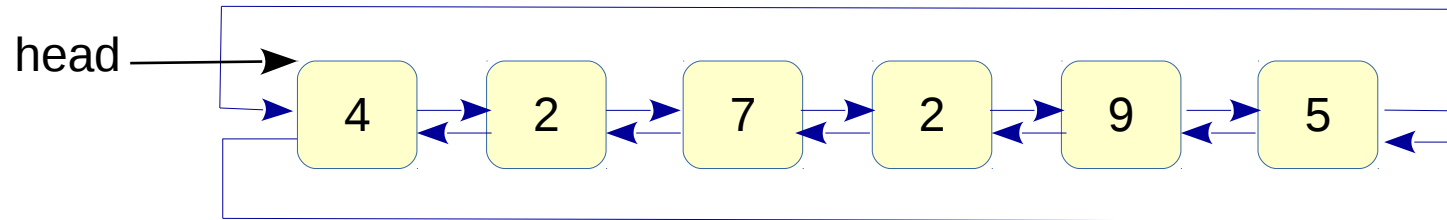
```
for (ptr = head; ptr; ptr = ptr->next)
    free(ptr); // invalid memory on free.
```

Doubly Linked List



- Links in both the directions.
- Node structure contains two pointers: next and previous.
- Deletion now becomes simpler.
- Two pointers: head and tail maintain list ends.
- **Classwork:** Write a function to remove a node.

Circular Doubly Linked List



- Last element points to the first, and first element's previous is the last node.
- Node structure continues to contain two pointers: next and previous.
- Tail pointer is **not** required.
- A singly linked list can also be circular.
- **Classwork:** Write a function to print all the node values in a CDLL.

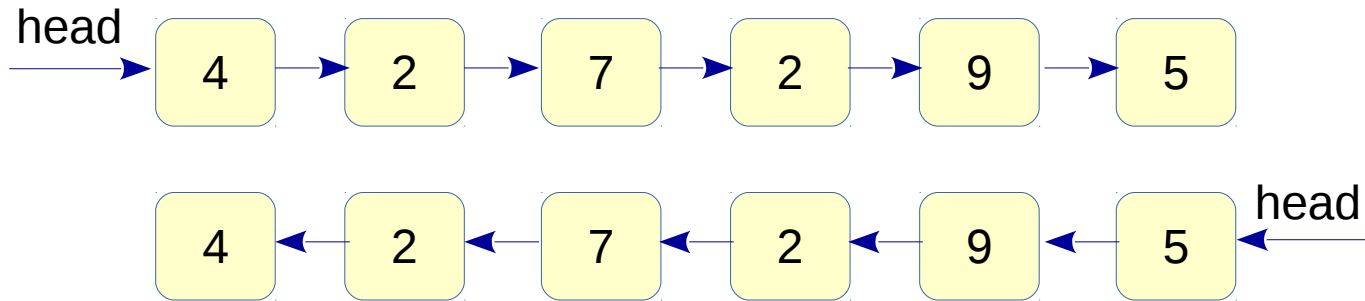
Polynomial ADT

- $F(X) = \sum_{i=0}^N A_i X^i$
- Example: $x^4 - 4x^3 + 7x - 6$
- **Member functions**
 - Initialize
 - Set a coefficient (for a power)
 - Add polynomials
 - Multiply polynomials
 - ...
- **Implementation**
 - Could be using arrays
 - Could be using linked lists
- **Classwork:** Create a struct / class to implement polynomials.
- Are there disadvantages of using arrays?
 - $2x^{1000} - x$
 - What are the design decisions for using lists?

Polynomial ADT

```
class Polynomial {  
    int coeff[MaxDegree + 1];  
};  
  
void Polynomial::initialize(int coeff[ ]) {  
    // Classwork: implement this.  
}  
  
void Polynomial::add(Polynomial p2, Polynomial psum) {  
    // Classwork: implement this.  
}
```

List Reversal



- Given a list (SLL, DLL, CSLL, CDLL), reverse it.
- The traversal from head should result in the opposite order.
- Typically need three pointers: previous, current and next.
- **Classwork:** Write a list reversal for SLL (*sll.cpp*).
- **Classwork:** Write a recursive list reversal.

Recursive Methods

- Sometimes natural to model.
- Sometimes inefficient to implement.
- **Classwork**: find an element recursively.
- **Classwork**: print a list recursively.
 - How to print in reverse?
 - **sl.cpp**

Stack ADT

- Special List
- Operations restricted to one end.
- Insert --> Push
- Remove --> Pop
- LIFO
- Cannot access arbitrary element.
- **Important:** Since this is ADT, we do not care about the implementation yet.

List versus Stack

```
class List {
```

```
    void insert(Element);
```

```
    void remove(Element);
```

```
    void search(Element);
```

```
    int size();
```

```
    void print();
```

```
    ...
```

```
};
```

```
class Stack {
```

```
    void push(Element);
```

```
    void pop(Element);
```

```
void search(Element);
```

```
int size(); bool isEmpty();
```

```
void print();
```

```
    ...
```

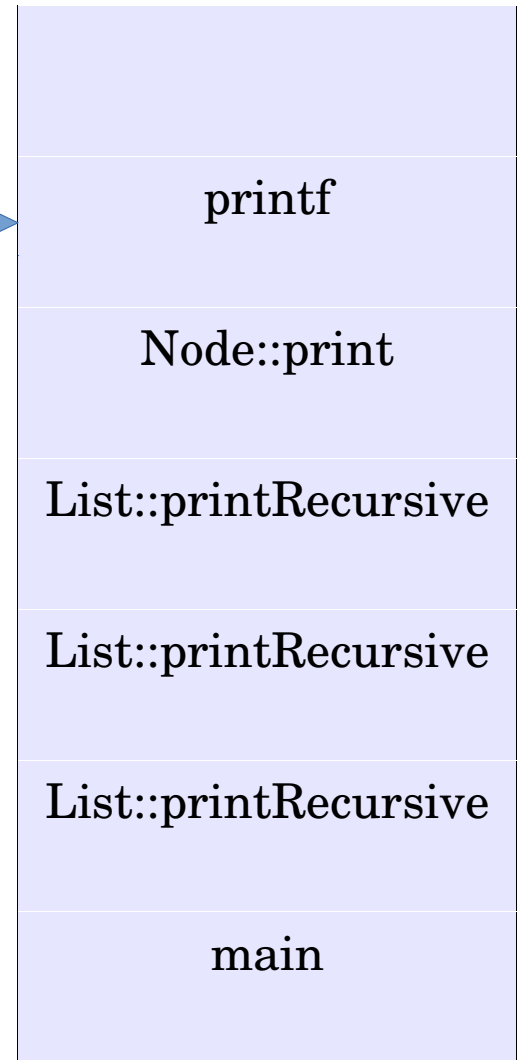
```
};
```

Stack Implementation

- **Design decisions**

- Array versus Linked List
- Allow traversing through the stack?
- Allow querying stack size?
- Allow peeking at the stack top?
- IsEmpty is user's responsibility or library implementation's?
- Stack Top points to the last element, or the entry next to that?

Stack top



Source: [stack.cpp](#)

Balanced Parentheses

- We want to check if parentheses are balanced or not.
- Three types of parentheses: (), [] and { }
- Valid inputs:
 - ([] [{ }])
 - [] { } [] () [[[]]]
- Invalid inputs:
 - ((())
 - ([)] { }
 - } }) ({ {

Classwork: Use stack to design an algorithm to check for balanced parentheses.

Question: Can we design an application of stack from its ADT without knowing its implementation?

Balanced Parentheses

for each input symbol c

if (c is an open parenthesis) `stack.push(c)`

else if (c is a close parenthesis) {

if `stack.top` contains the matching open parenthesis

pop the element from stack

else error

Find a string to match
this error.

}

Source: `parentheses.cpp`

if (stack is empty)

// all good.

else error

Find a string to match
this error.

Stack Implementation

- `stackimpl.c`

Expressions

- $1 + 2 * 3 - 4$

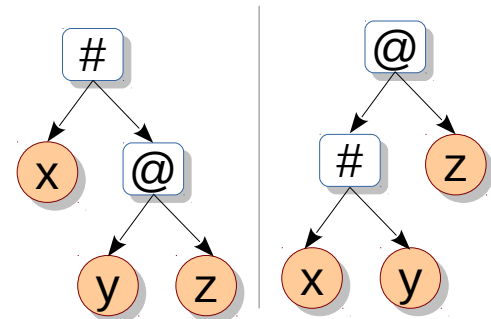
- Binary operators appear **between** the operands
- Ambiguous without extra knowledge

$(1 + 2) * (3 - 4)$ OR

$1 + (2 * (3 - 4))$ OR

$(1 + (2 * 3)) - 4$ OR

$((1 + 2) * 3) - 4$?



- Parentheses help disambiguate; domain knowledge helps disambiguate (operator precedence).
- Won't it be nice if expressions can be written in unambiguous manner?

Prefix and Postfix Forms

- $1 + 2 * 3 - 4$
 - Binary operators appear **between** the operands.
 - Called as **infix** form.
- $1\ 2\ 3\ * + 4\ -$
 - Binary operators appear **after** the operands.
 - Called as **postfix** form.
- $- + 1\ * 2\ 3\ 4$
 - Binary operators appear **before** the operands.
 - Called as **prefix** form.

How do these forms help resolve ambiguity?

Prefix, Postfix and Non-ambiguity

Infix	Prefix	Postfix
$(1 + 2) * (3 - 4)$		
$1 + (2 * (3 - 4))$		
$(1 + (2 * 3)) - 4$		
$((1 + 2) * 3) - 4$		
$1 + ((2 * 3) - 4)$		

Prefix, Postfix and Non-ambiguity

Infix	Prefix	Postfix
$(1 + 2) * (3 - 4)$	$* + 1 2 - 3 4$	$1 2 + 3 4 - *$
$1 + (2 * (3 - 4))$	$+ 1 * 2 - 3 4$	$1 2 3 4 - * +$
$(1 + (2 * 3)) - 4$	$- + 1 * 2 3 4$	$1 2 3 * + 4 -$
$((1 + 2) * 3) - 4$	$- * + 1 2 3 4$	$1 2 + 3 * 4 -$
$1 + ((2 * 3) - 4)$	$+ 1 - * 2 3 4$	$1 2 3 * 4 - +$

- No parentheses in prefix and postfix forms.
- Infix is ambiguous; prefix and postfix are not.
- Unique prefix and postfix forms for different orders of operator evaluation.

Postfix Evaluation

- Find the value of $5\ 1\ 2\ 3\ *\ -\ 4\ +\ 6\ *\ -$.
- Write a program to evaluate a postfix expression.
 - Assume digits, +, −, *, /.

For each symbol in the expression
If the symbol is an **operand**
 Push its value to a stack
Else if the symbol is an **operator**
 Pop two nodes from the stack
 Apply the operator on them
 Push result to the stack

Source: postfixeval.cpp

Prefix Evaluation

For each symbol in the expression right-to-left

If the symbol is an **operand**

Push its value to the stack

Else if the symbol is an **operator**

Pop two symbols from the stack

Apply the operator on them

Push result to the stack

Prefix

* + 1 2 - 3 4

+ 1 * 2 - 3 4

- + 1 * 2 3 4

- * + 1 2 3 4

+ 1 - * 2 3 4

Homework: Code this up.

Infix to Postfix

- Given an infix expression (with parentheses), convert it to a postfix form (without parentheses).

Infix	Prefix	Postfix
$(1 + 2) * (3 - 4)$	$* + 1 2 - 3 4$	$1 2 + 3 4 - *$
$1 + (2 * (3 - 4))$	$+ 1 * 2 - 3 4$	$1 2 3 4 - * +$
$(1 + (2 * 3)) - 4$	$- + 1 * 2 3 4$	$1 2 3 * + 4 -$
$((1 + 2) * 3) - 4$	$- * + 1 2 3 4$	$1 2 + 3 * 4 -$
$1 + ((2 * 3) - 4)$	$+ 1 - * 2 3 4$	$1 2 3 * 4 - +$

For each symbol in the expression

If the symbol is an **operand**

Print the symbol

Else if the symbol is an **opening parenthesis**

Push the symbol on stack

Else if the symbol is a **closing parenthesis**

Do {

Pop symbol from the stack

If symbol is not opening parenthesis

Print the symbol

} while symbol is not opening parenthesis

Else { // symbol c is an **operator**

Pop symbol d from the stack

While symbol d has higher or equal priority than c

Print the symbol d

Pop symbol d from the stack

Push the symbol on stack

}

}

While stack is not empty {

Pop symbol from the stack

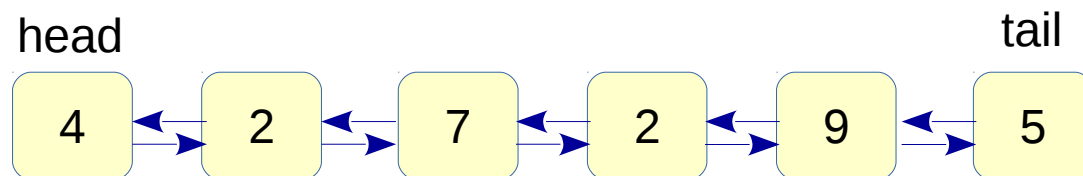
Print the symbol

}

Return postfix

Queue

- Special list
- Insertions at one end, deletions at the other
- Tracked using two pointers: head and tail
- FIFO (what is FCFS?)
- Cannot access arbitrary element
- Insert → push / enqueue
remove → pop / dequeue



Queue ADT

- **Classwork:** Write down the Queue ADT.

```
struct Queue {  
    void push(Element);    // enqueue  
    Element pop();        // dequeue  
    bool isEmpty();  
    ...  
};
```

```
class Queue {  
    void push(Element);  
    void pop();  
    Element front();  
    Element back();  
    bool isEmpty();  
    ...  
};
```

Source: q.cpp

Call Center

- Multiple users call a call-center.
- Multiple operators answer the call.
- Each call takes an unknown amount of time.
- When all the operators are busy
 - Calling users need to wait.
- When an operator becomes available
 - Which waiting user is answered?
- Can we use Queue ADT to implement this?

Call Center: Data Structures

- User (id, call time)
- Operator (id)
- Queue of waiting users
- List of busy operators
- Queue of free operators

Call Center: Simulation

- Simulation is often based on time.
- At each time unit, various actions occur.
 - A new user arrives.
 - A free operator needs to be assigned to a user.
 - No operator is free, so the user needs to wait.
 - A busy operator becomes free.
 - Nothing happens, call time of engaged users reduces.
- Simulation ties these actions together logically.

Source: callcenter.cpp

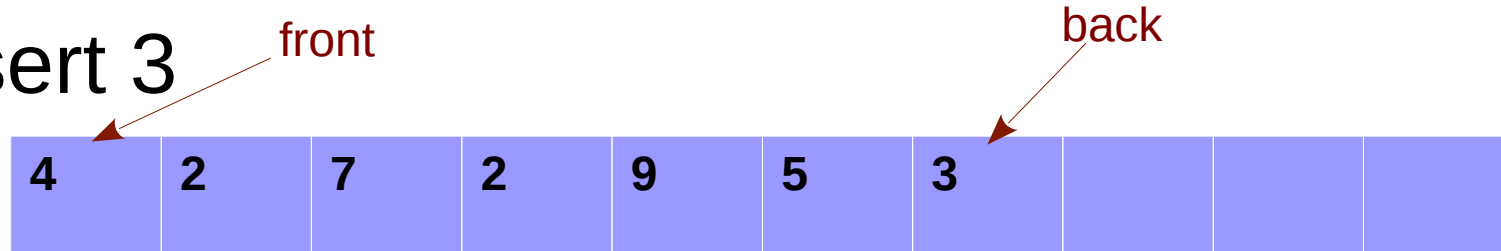
Queue Implementation

Recall
circular list

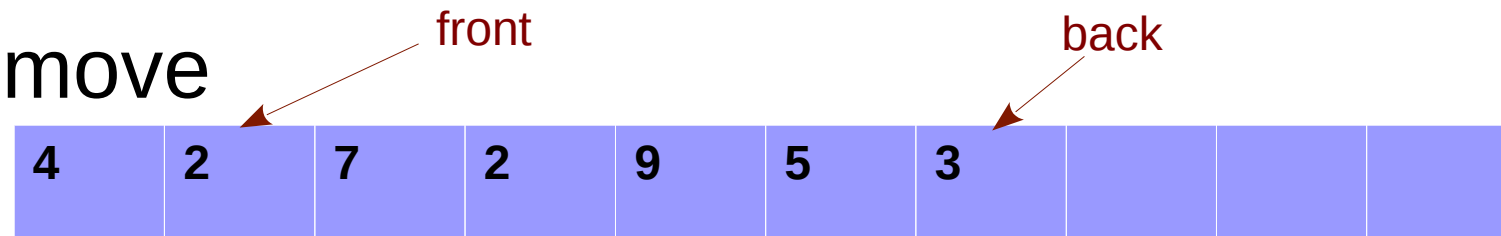
- This time, we will use arrays.



- Insert 3

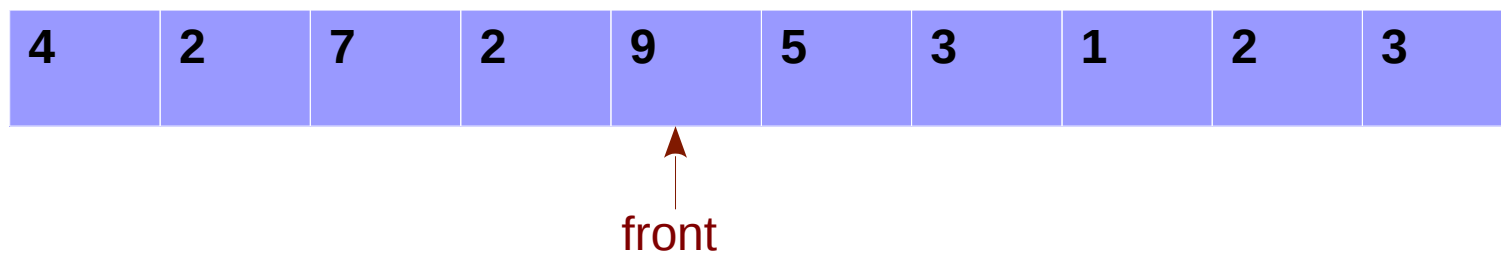


- Remove



qimpl.c


- Remove, Remove, Remove, Insert 1, 2, 3, 4



Wrap-around

- Insert 4
-
- | | | | | | | | | | |
|---|--|--|--|---|---|---|---|---|---|
| 4 | | | | 9 | 5 | 3 | 1 | 2 | 3 |
|---|--|--|--|---|---|---|---|---|---|

- Remove five elements, Insert 2
-
- The diagram shows a horizontal array of 10 light blue squares representing a queue. The first square contains the number 4, the second contains 2, and the tenth (last) square contains 3. A red arrow labeled 'back' points to the first square. A red arrow labeled 'front' points to the last square.

- Remove
 

- Remove

- Remove

back

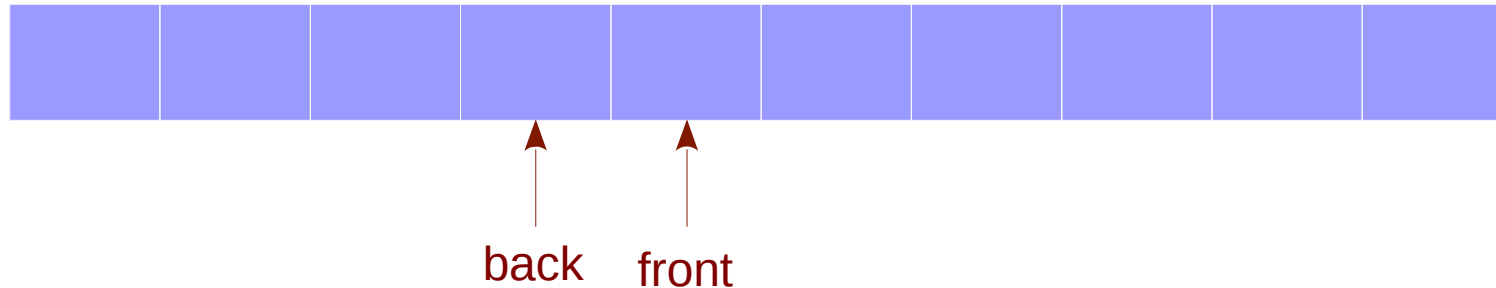
back front

Queue Conditions

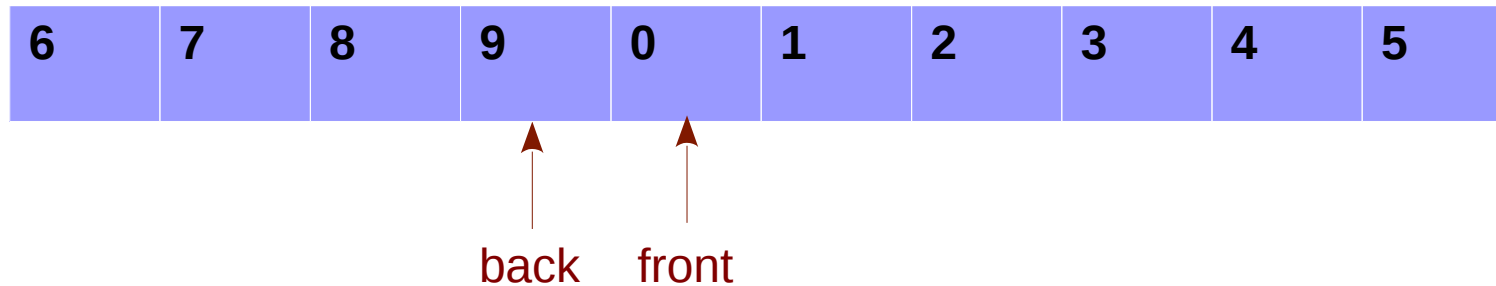
- Queue is empty:
 - when $\text{front} > \text{back}$ (in previous slide)
 - That is also initialization: $\text{front} = 0, \text{back} = -1$
 - Our implementation **qimpl.c** uses $\text{front} = 0, \text{back} = 0$
- Whichever you use, follow invariants:
 - **qimpl.c**: front points to the first element in the queue.
 back points to the place where next element should be inserted.
 - Previous slide: front points to the first element in the queue.
 back points to the last element in the queue.
- **Classwork**: Write conditions for when queue is full.

Empty versus Full

- Empty queue



- Full queue



- Possible solutions

- Leave one space unused ($N-1$ elements).
- Track size separately (used in `qimpl.c`).

Practice problems

- Implement a stack using two queues.
 - push/pop should be implemented using enqueue / dequeue.
- Implement a queue using two stacks.
- Implement three stacks using an array (without space wastage).
- Solve problems at the end of Chapter 3.

Learning Outcomes

- Use List, Stack, Queue ADTs in applications.
- Implement these ADTs using C/C++ with pointers or arrays.
- Study various applications using these data structures.